

# Neutrinoless double beta decay with *light* sterile neutrinos

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JHEP06(2020)097

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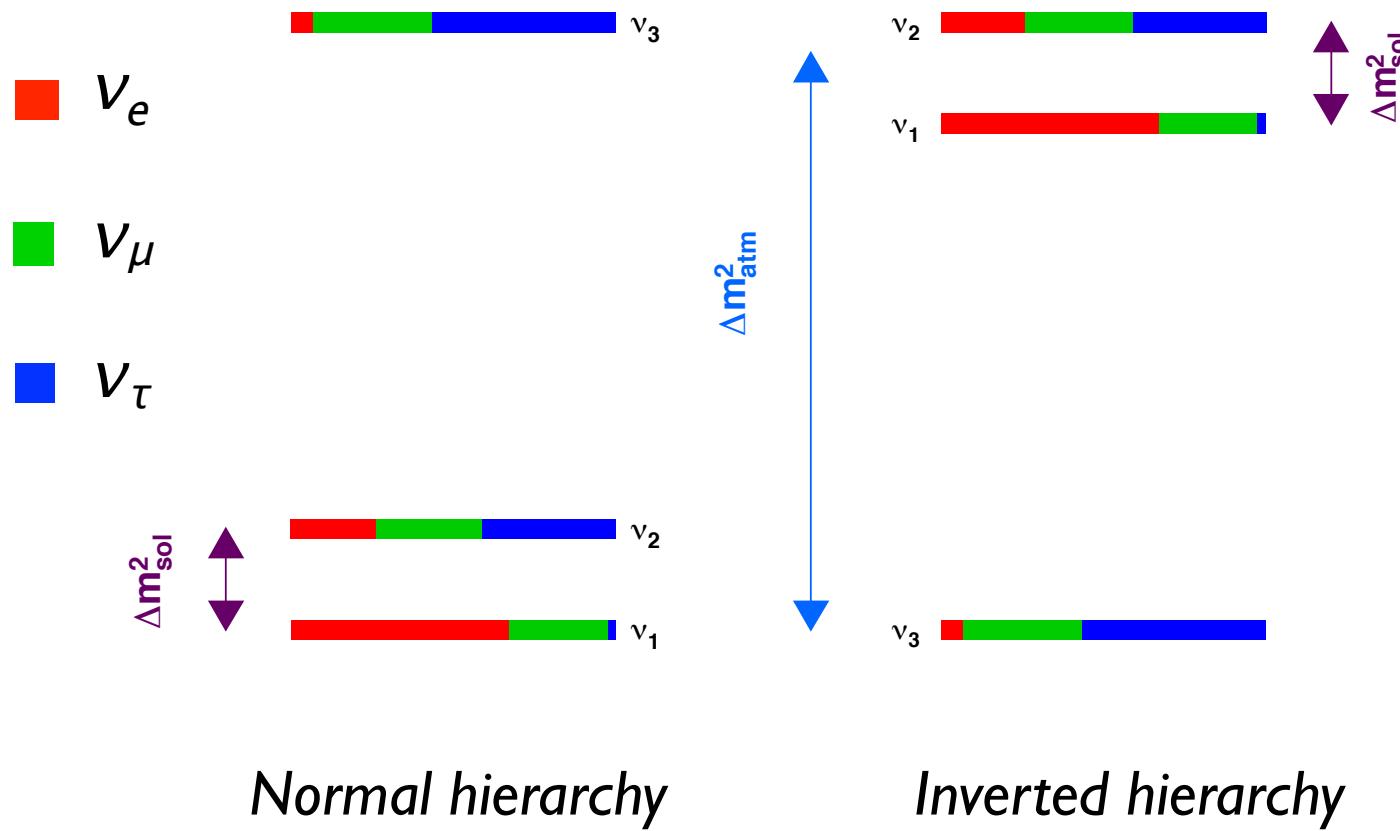
# Outline :

- I. Introduction
2. Neutrinoless double beta decay
  - *EFT approach with light sterile neutrino*
3. Standard vs Non-standard interactions
4. Summary

# *Introduction*

# Neutrino mass

The observation of neutrino oscillation confirms neutrinos have mass.

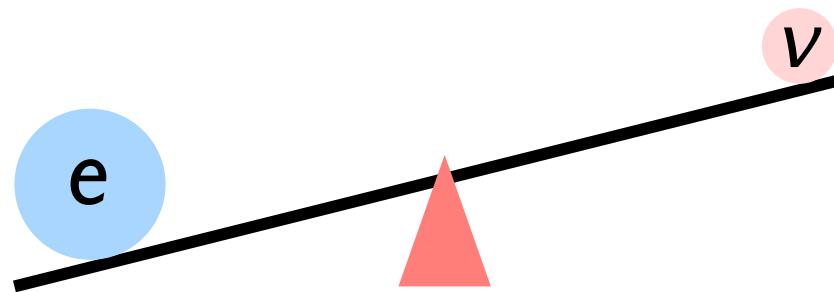


# Neutrino mass

The observation of neutrino oscillation confirms neutrinos have mass.

Ex)

Electron : 0.5 MeV       $< 1 \text{ eV}$

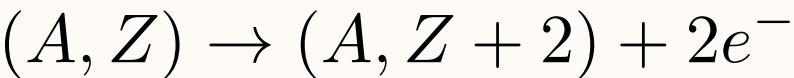


Open question :

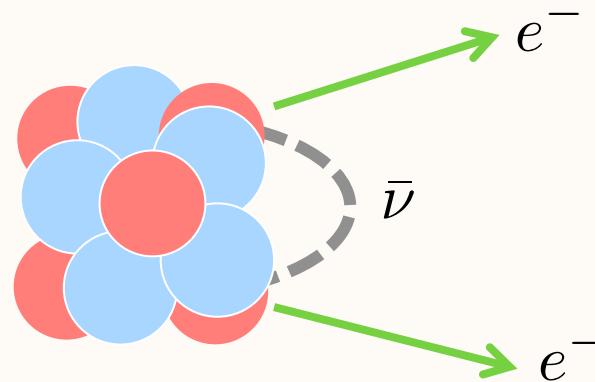
*What is the origin of the tiny but non-vanishing masses of the neutrinos?*

# Neutrinoless double beta decay

Double  $\beta$  decay without neutrino emission



Nuclei



The process can occur if neutrino is a *Majorana* particle.

# Majorana mass

Right-handed neutrino :  $\nu_R$

~ Gauge singlet (Sterile neutrino)

$$\mathcal{L}_{\nu_R} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \text{H.C}$$


---

$$L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}, \quad H = \begin{pmatrix} G^+ \\ \frac{1}{2}(v + h) \end{pmatrix}, \quad v \simeq 246 \text{ GeV}$$

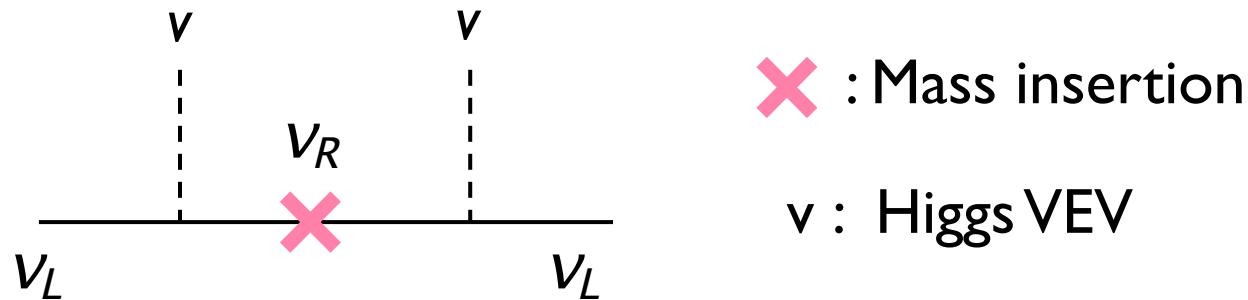
$$\nu_R^c = C \overline{\nu_R}^T \quad \text{C : charge conjugation matrix}$$

# Majorana mass

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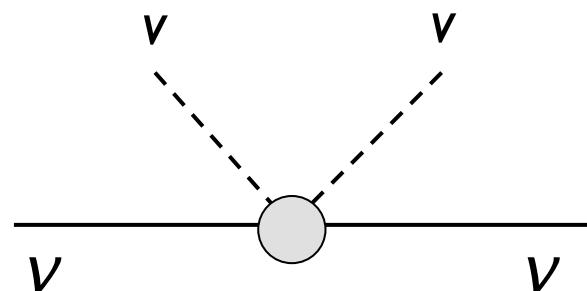
# Majorana mass

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*Majorana mass term is induced.*



$$\mathcal{L}_{\text{mass}} = -\frac{1}{2} \bar{\nu} m_\nu \nu$$

$$(\nu = \nu^c)$$

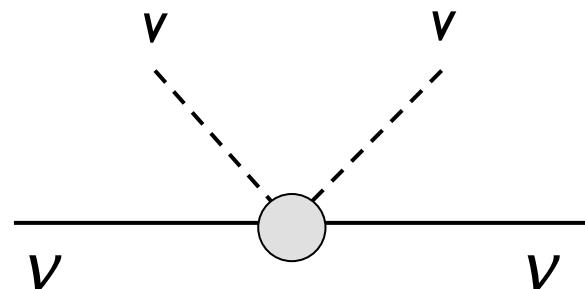
# Majorana mass

Right-handed neutrino :  $\nu_R$

~ Gauge singlet (Sterile neutrino)

Yukawa	Majorana Mass
$\mathcal{L}_{\nu_R} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \text{H.C}$	

If  $M_R$  is much heavier than EW scale,



$$m_\nu \sim \frac{Y_\nu^2 v^2}{M_R}$$

# Majorana mass

Right-handed neutrino :  $\nu_R$

~ Gauge singlet (Sterile neutrino)

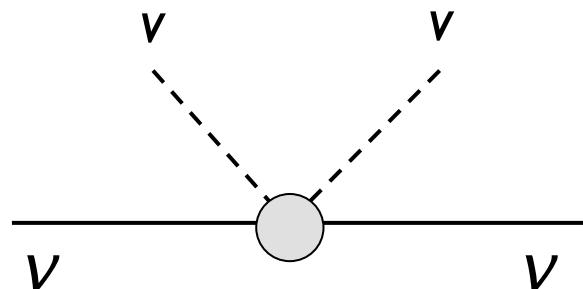
*Yukawa*

*Majorana Mass*

1

If neutrinos are Majorana particles,  $0\nu2\beta$  is induced.

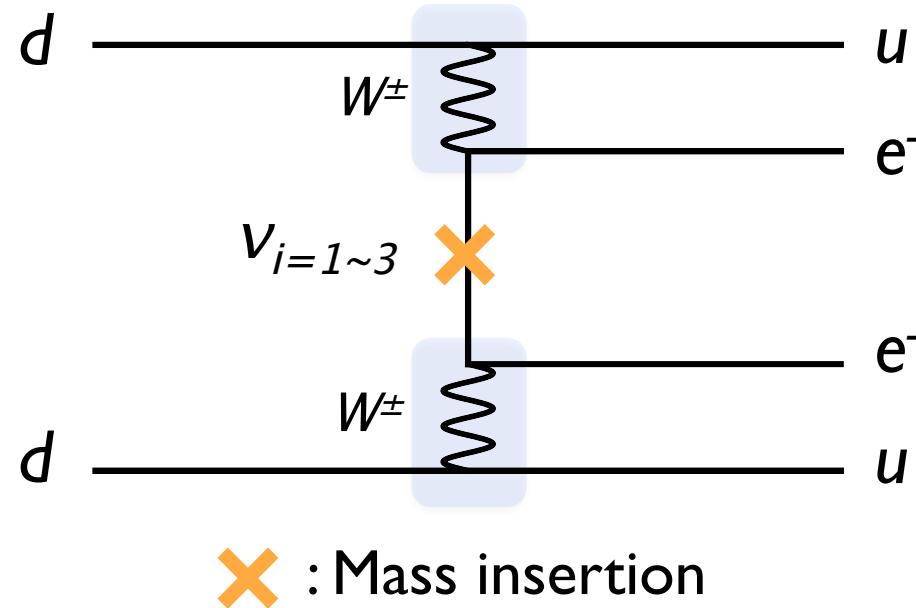
\* Three light Majorana neutrino case ( $M_R \gg v$ )



$$m_\nu \sim \frac{Y_\nu^2 v^2}{M_R}$$

# Standard case

Three light Majorana neutrinos :  $\nu_{i=1 \sim 3}$

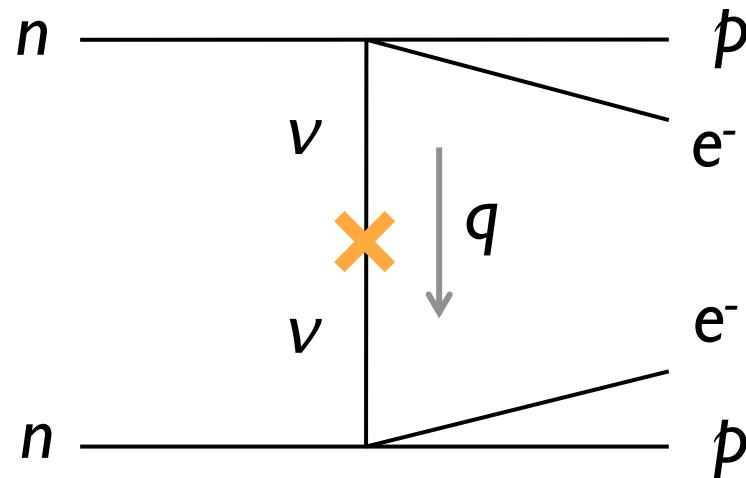


*Left-handed vector operator :*

$$\mathcal{L}^{(6)} = \frac{G_F}{\sqrt{2}} \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu C_{\text{VLL}}^{(6)} \nu \quad | \quad C_{\text{VLL}}^{(6)} = -2V_{ud}U_{ei}$$

# Standard case

Three light Majorana neutrinos :  $\nu_{i=1 \sim 3}$

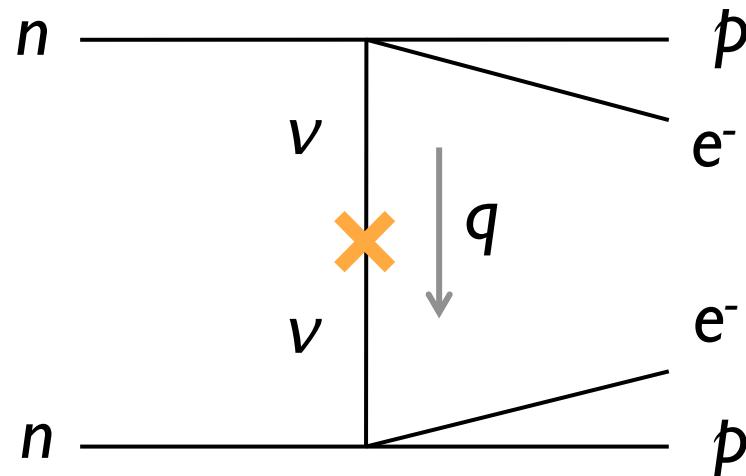


$$\mathcal{A}_{0\nu 2\beta} \sim \sum_{i=1}^3 U_{ei}^2 \frac{m_i}{q^2 + m_i^2} \sim \frac{1}{q^2} \left( \sum_{i=1}^3 U_{ei}^2 m_i \right)$$

$\mathcal{O}(100) \text{ MeV}$

# Standard case

Three light Majorana neutrinos :  $\nu_{i=1 \sim 3}$



Oscillation data

$$\mathcal{A}_{0\nu2\beta} \sim \sum_{i=1}^3 U_{ei}^2 \frac{m_i}{q^2 + m_i^2} \sim \frac{1}{q^2} \left( \sum_{i=1}^3 U_{ei}^2 m_i \right)$$

$\mathcal{O}(100)$  MeV

Effective mass :  $m_{\beta\beta}$

# Standard case

Oscillation data : PRD98(2018)030001 [PDG]

$$U_{\text{PMNS}} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ \cdots & \cdots & \cdots \\ \cdots & \cdots & \cdots \end{pmatrix}$$

$$\Delta m_{21}^2 = m_2^2 - m_1^2 = 7.39 \times 10^{-5} \text{ [eV}^2]$$

$$\Delta m_{31}^2 = m_3^2 - m_1^2 = \pm 2.5 \times 10^{-3} \text{ [eV}^2]$$

*Ex) Normal hierarchy case*

$$\mathcal{A}_{0\nu 2\beta} \propto \left[ c_{13}^2 \left( m_1 c_{12}^2 + e^{i\alpha} s_{12}^2 \sqrt{m_1^2 + \Delta m_{21}^2} \right) + e^{i\beta} s_{13}^2 \sqrt{m_1^2 + \Delta m_{31}^2} \right]$$

✓ The amplitude is described by the lightest neutrino mass.

# Standard case

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Inverse half-life :  $\left(T_{1/2}^{0\nu}\right)^{-1} = g_A^4 G_{0\nu} |\mathcal{A}_{0\nu 2\beta}|^2$

$g_A = 1.27$ ,  $G_{0\nu}$  : Phase space factor

# Search for $0\nu2\beta$

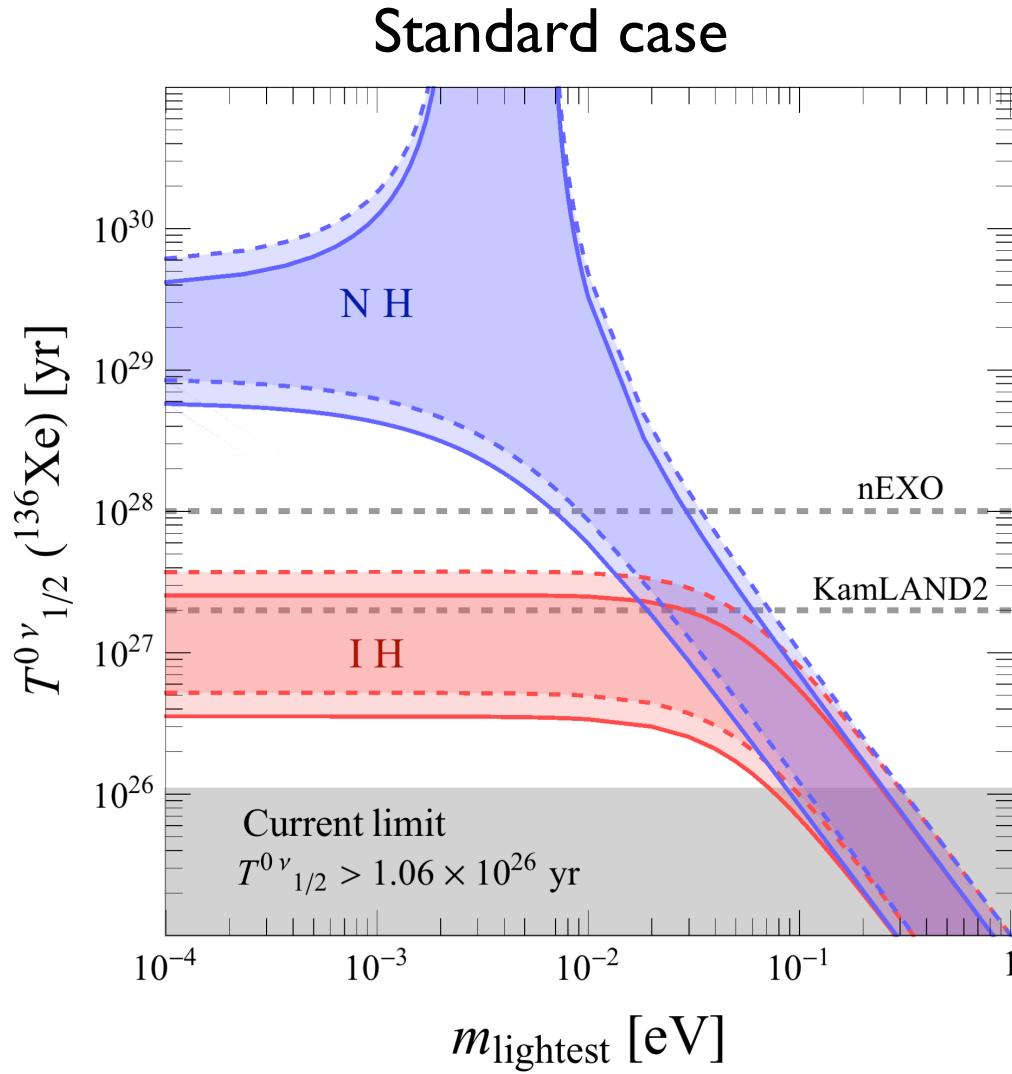


Isotope	Experiment	Current limit ( $\times 10^{25}$ yr)	Future sensitivity ( $\times 10^{25}$ yr)
$^{48}\text{Ca}$	ELEGANT-IV	$5.8 \times 10^{-3}$	[2]
	CANDLES	$6.2 \times 10^{-3}$	[23]
	NEMO-3	$2.0 \times 10^{-3}$	[9]
$^{76}\text{Ge}$	MAJORANA DEMONSTRATOR	2.7	[22]
	GERDA	9.0	[24]
	LEGEND	—	$10^3$ [29]
$^{82}\text{Se}$	CUPID	$3.5 \times 10^{-1}$	[25]
	NEMO-3	$2.5 \times 10^{-2}$	[20]
	SuperNEMO	—	10 [30]
$^{96}\text{Zr}$	NEMO-3	$9.2 \times 10^{-4}$	[3]
$^{100}\text{Mo}$	NEMO-3	$1.1 \times 10^{-1}$	[8]
	CUPID-1T	—	$9.2 \times 10^2$ [37]
	AMoRE	$9.5 \times 10^{-3}$	[26]
$^{116}\text{Cd}$	NEMO-3	$1.0 \times 10^{-2}$	[13]
$^{128}\text{Te}$	—	$1.1 \times 10^{-2}$	[1]
$^{130}\text{Te}$	CUORE	3.2	[21]
	SNO+	—	$1.0 \times 10^2$ [33]
$^{136}\text{Xe}$	KamLAND-Zen	10.7	[10]
	EXO-200	3.5	[27]
	NEXT	—	$2.0 \times 10^2$ [35]
	PandaX	—	$1.0 \times 10^2$ [36]
$^{150}\text{Nd}$	NEMO-3	$2.0 \times 10^{-3}$	[12]

$$T_{1/2}^{0\nu} ({}^{136}\text{Xe}) > 1.06 \times 10^{26} \text{ yr}$$

KamLAND-Zen  
PRL117(2016) 082503

# Current limit on half-life



*Normal Hierarchy (NH)*

$$m_1 < m_2 < m_3$$

*Inverted Hierarchy (IH)*

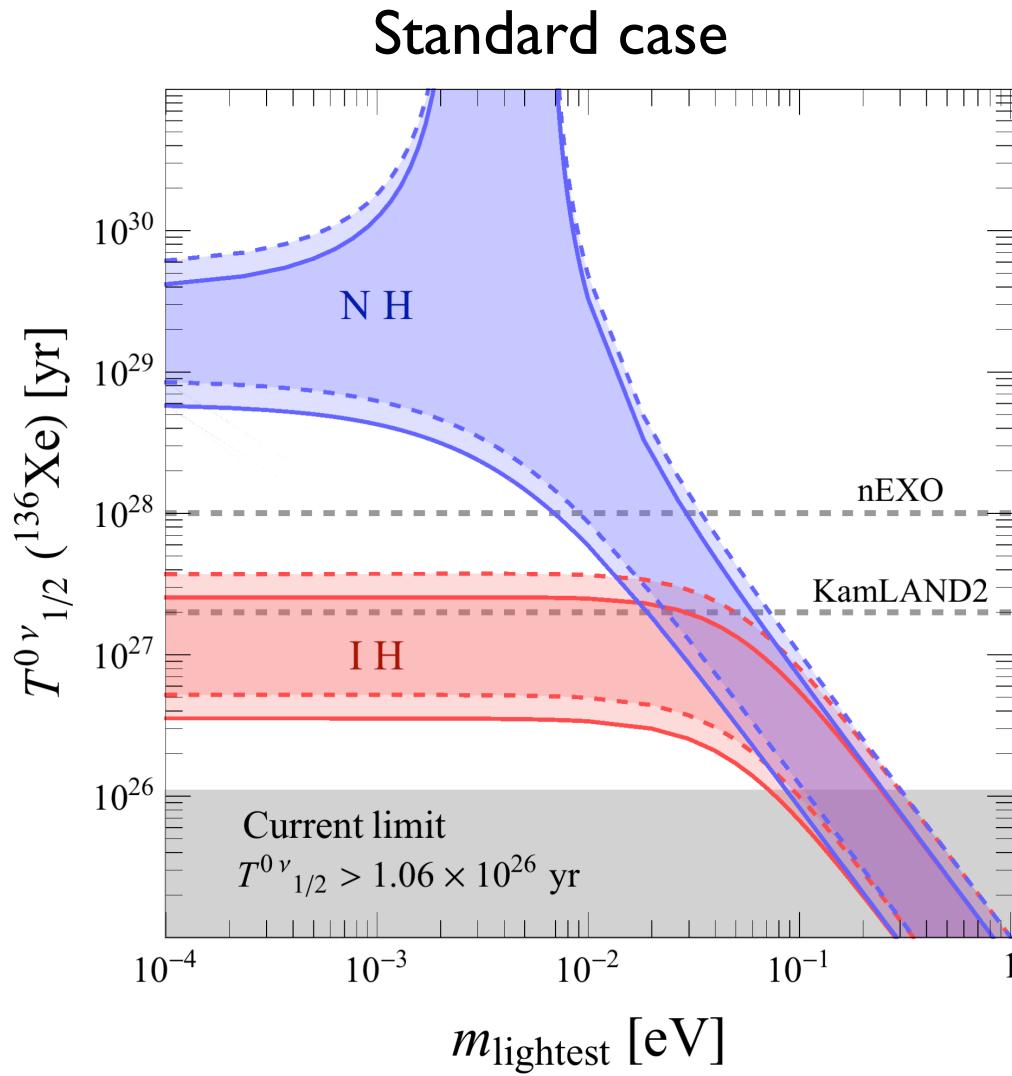
$$m_3 < m_1 < m_2$$

\* Bands

I) Majorana phase

2) Matrix elements

# Current limit on half-life



*Normal Hierarchy (NH)*

$$m_1 < m_2 < m_3$$

*Inverted Hierarchy (IH)*

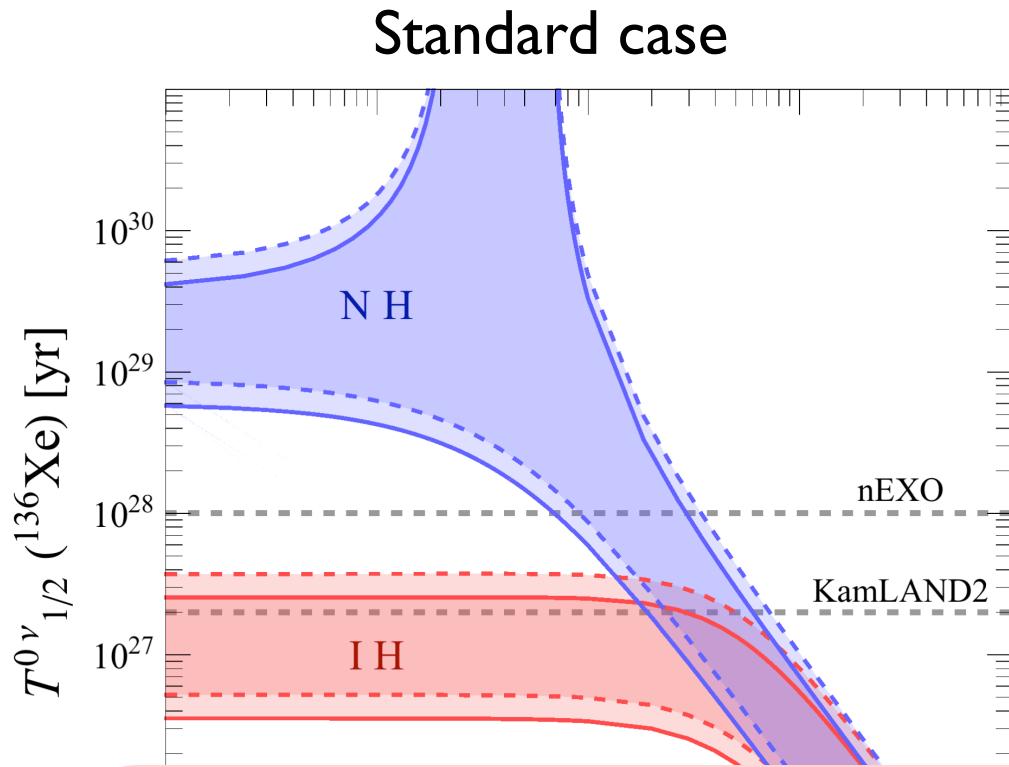
$$m_3 < m_1 < m_2$$

★ *Future sensitivity*

$\sim 10^{27} \text{ yr} : \text{KamLAND2-Zen}$

$\sim 10^{28} \text{ yr} : \text{nEXO}$

# Current limit on half-life



**Normal Hierarchy (NH)**

$$m_1 < m_2 < m_3$$

**Inverted Hierarchy (IH)**

$$m_3 < m_1 < m_2$$

Future sensitivity

*Standard case : Three light Majorana neutrinos ( $M_R \gg v$ )*

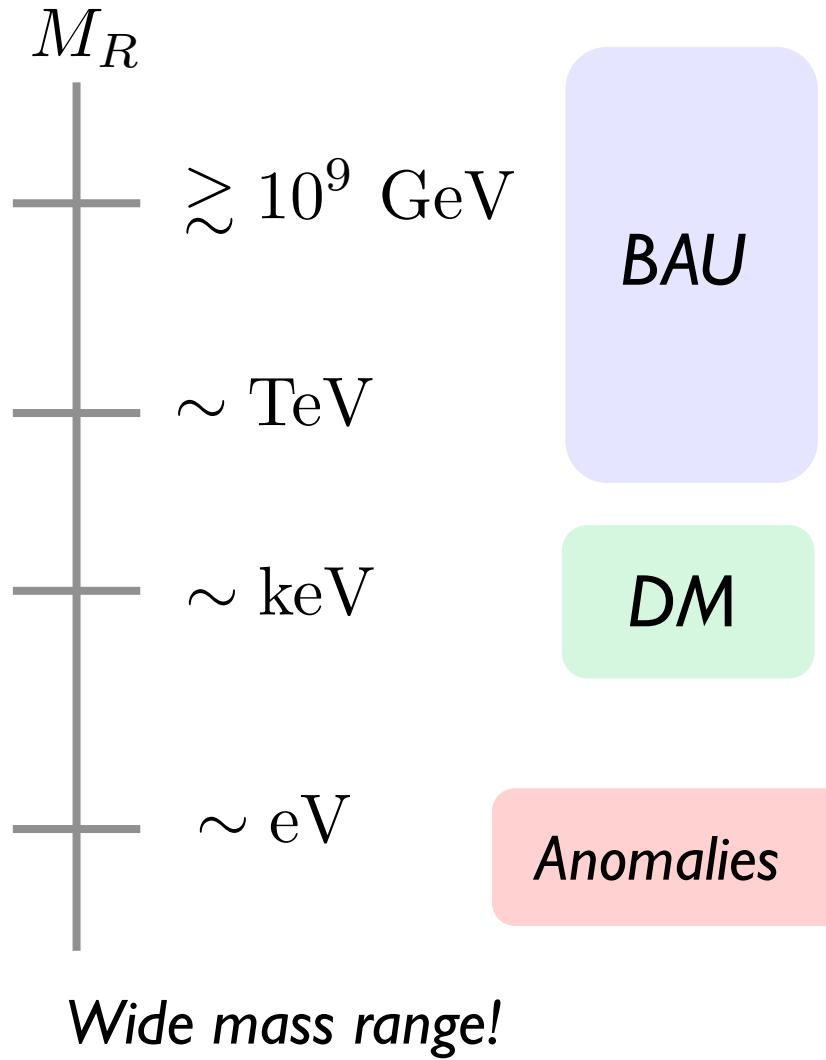
*What about light  $M_R$  case?*

# Beyond the standard case

For more details, see  
M. Drewes, 1303.6912

21

Other phenomenological aspects:



*Leptogenesis*

W. Buchmuller, et al , Ann.Rev.Nucl.Part.Sci.  
55 (2005)311,

E. K.Akhmedov, et al, PRL81(1998)1359  
T.Asaka, et al, PLBB620, 17 (2005),

*DM candidate*

S. Dodelson, L. M. Widrow, PRL72(1994)17  
T.Asaka, et al, PLBB638, 401 (2006),

*Short-baseline neutrino oscillation*

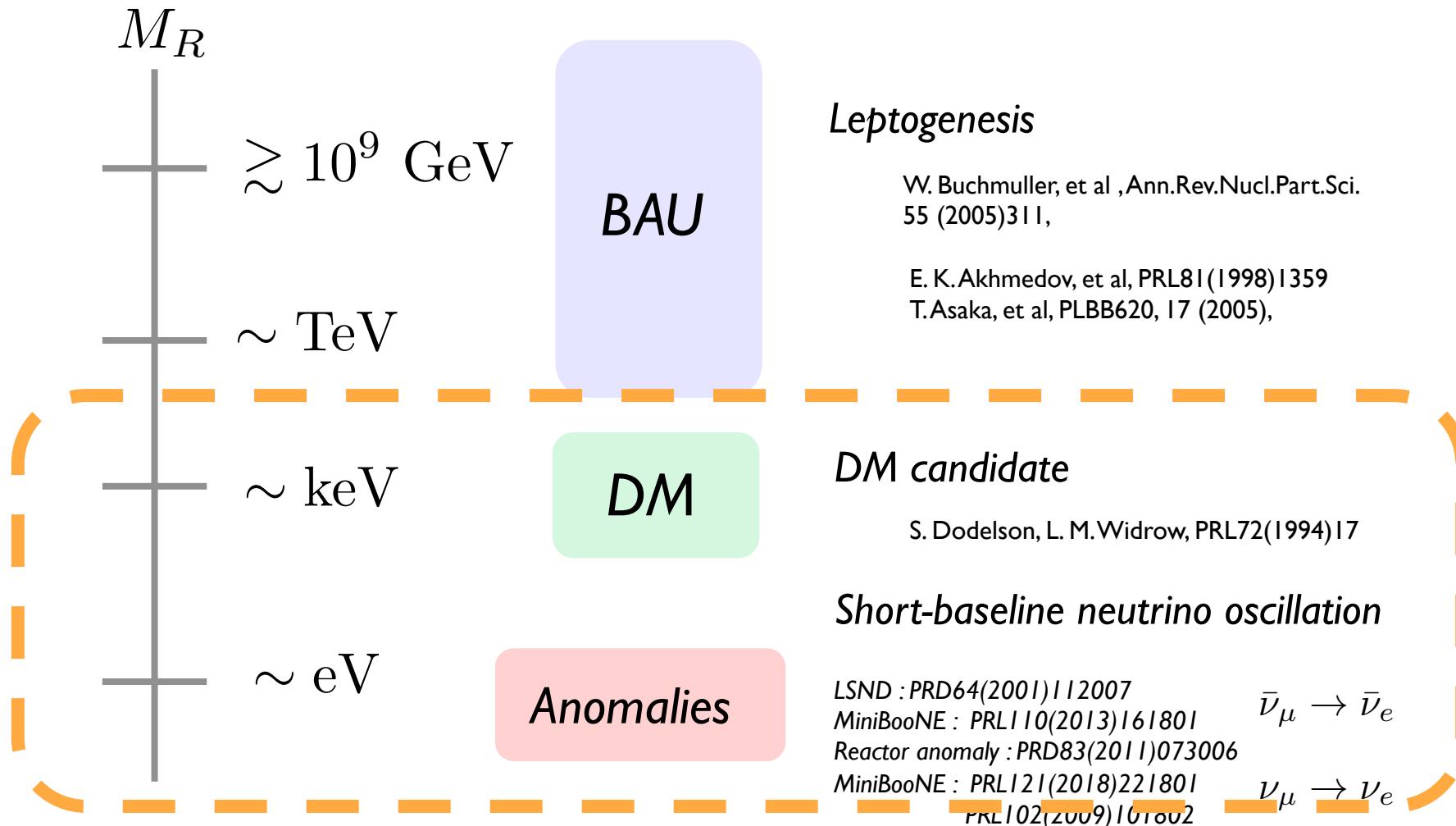
LSND : PRD64(2001)112007  
MiniBooNE : PRL110(2013)161801       $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$   
Reactor anomaly : PRD83(2011)073006  
MiniBooNE : PRL121(2018)221801       $\nu_\mu \rightarrow \nu_e$   
PRL102(2009)101802

# Beyond the standard case

For more details, see  
M. Drewes, 1303.6912

22

\* Need theoretical analysis in light of light sterile neutrinos



# Our study

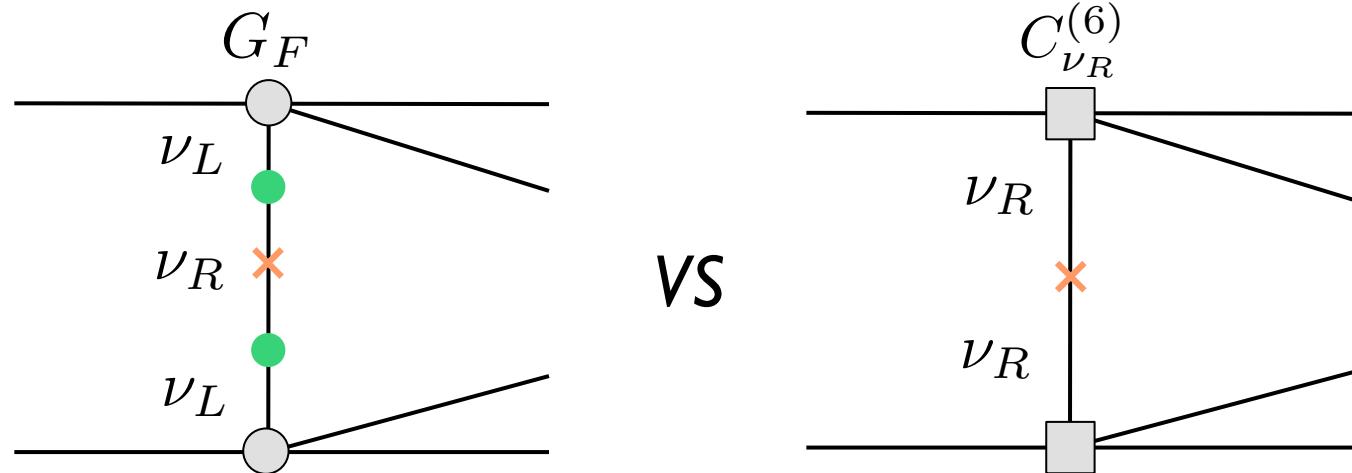
- ★ Model-independent analysis in the light  $\nu_R$  scenario  
~ *Effective Field Theory*

# Our study

★ Model-independent analysis in the light  $\nu_R$  scenario  
 $\sim$  *Effective Field Theory*

\* Non-standard interactions ( $d = 6$ )

$$\mathcal{L} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \frac{1}{\Lambda^2} C_{\nu_R}^{(6)} \mathcal{O}^{(6)}$$



# Our study

- ★ Model-independent analysis in the light  $\nu_R$  scenario  
~ *Effective Field Theory*

- \* Non-standard interactions ( $d = 6$ )

$$\mathcal{L} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \frac{1}{\Lambda^2} C_{\nu_R}^{(6)} \mathcal{O}^{(6)}$$

- \* Derive the master formula depending on  $M_R$

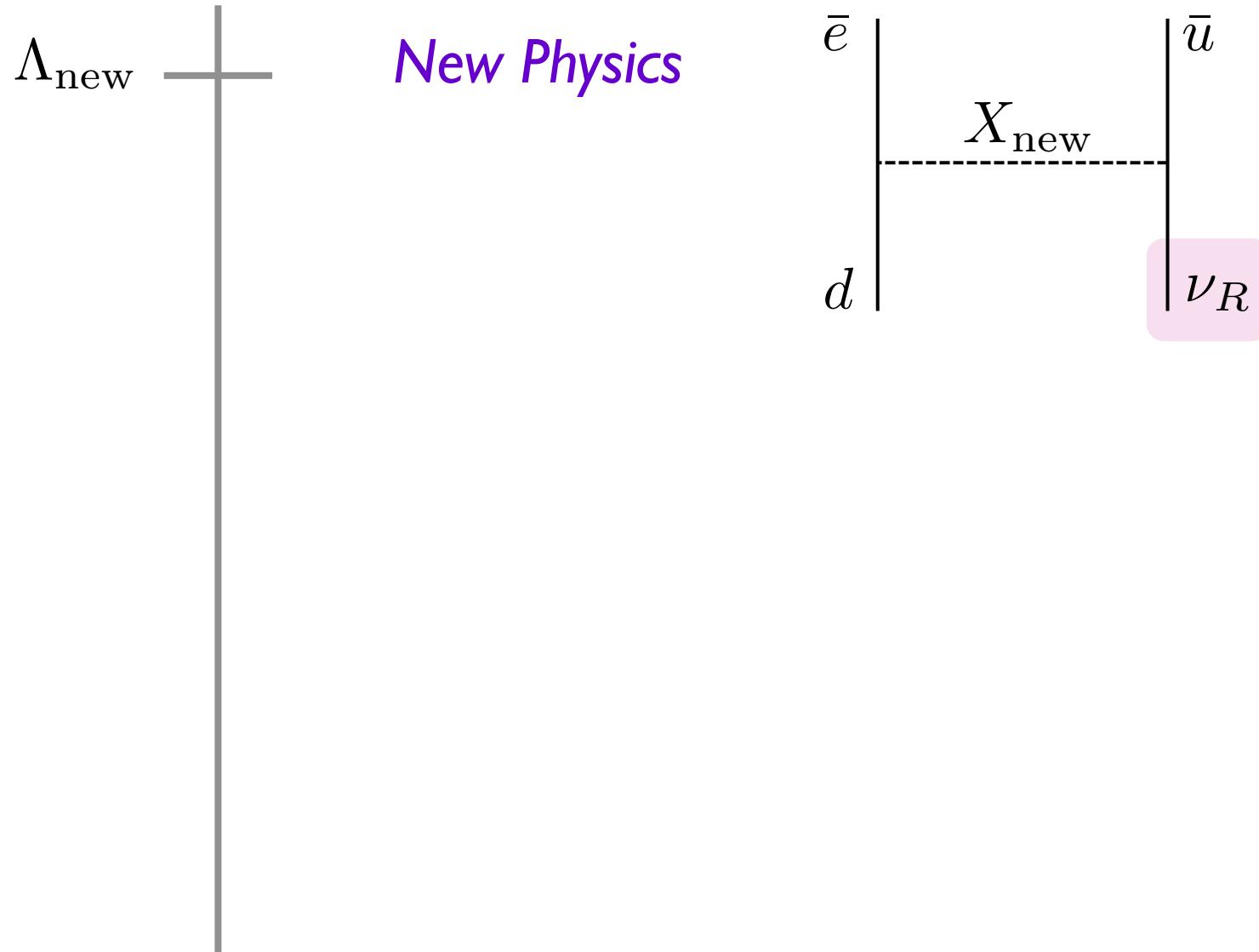
Mass range :  $M_R$   
eV  $\longleftrightarrow$   $10^{15}$ GeV

Capture the behavior of light- and high-mass neutrino

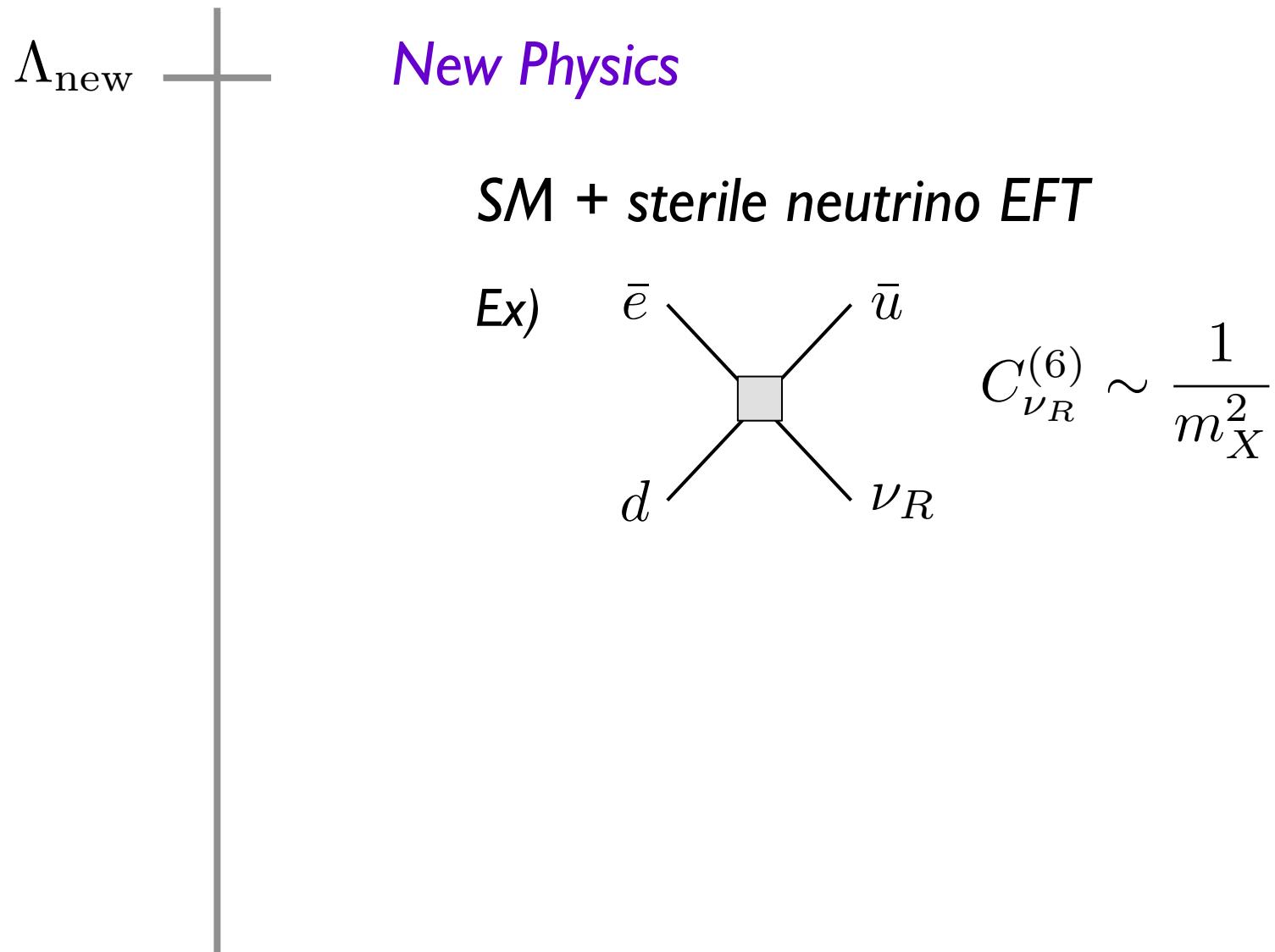
*SM + Light sterile neutrinos EFT*

# EFT approach

G. Prezeau, M. Ramsey-Musolf, and P. Vogel, PRD68, 034016 (2003)  
V. Cirigliano, W. Dekens, J. de Vries, M. L. Graesser, and E. Mereghetti, JHEP 12, 082(2017)  
V. Cirigliano, W. Dekens, J. de Vries, M. L. Graesser, and E. Mereghetti, JHEP 12, 097(2018)



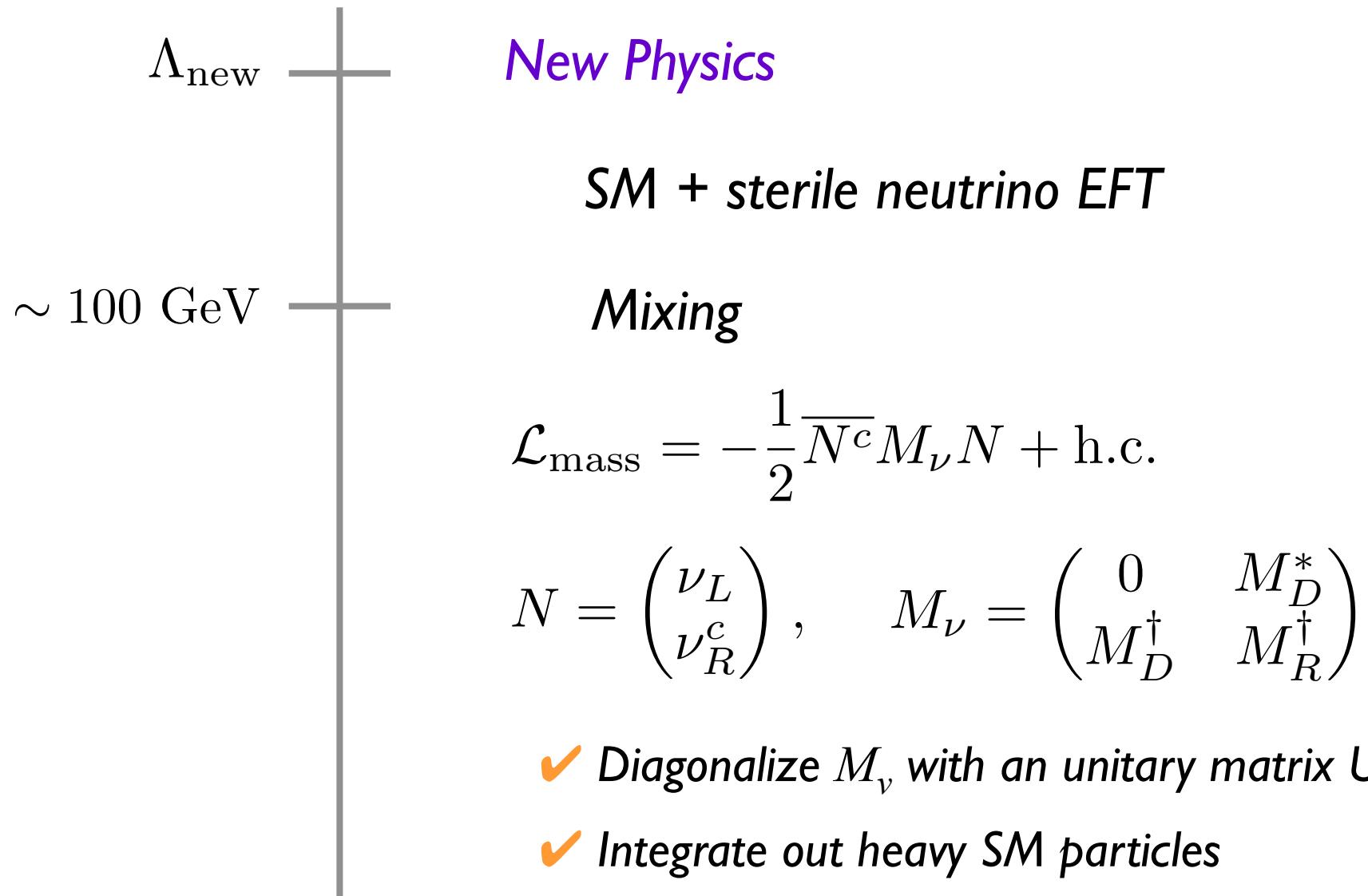
# EFT approach



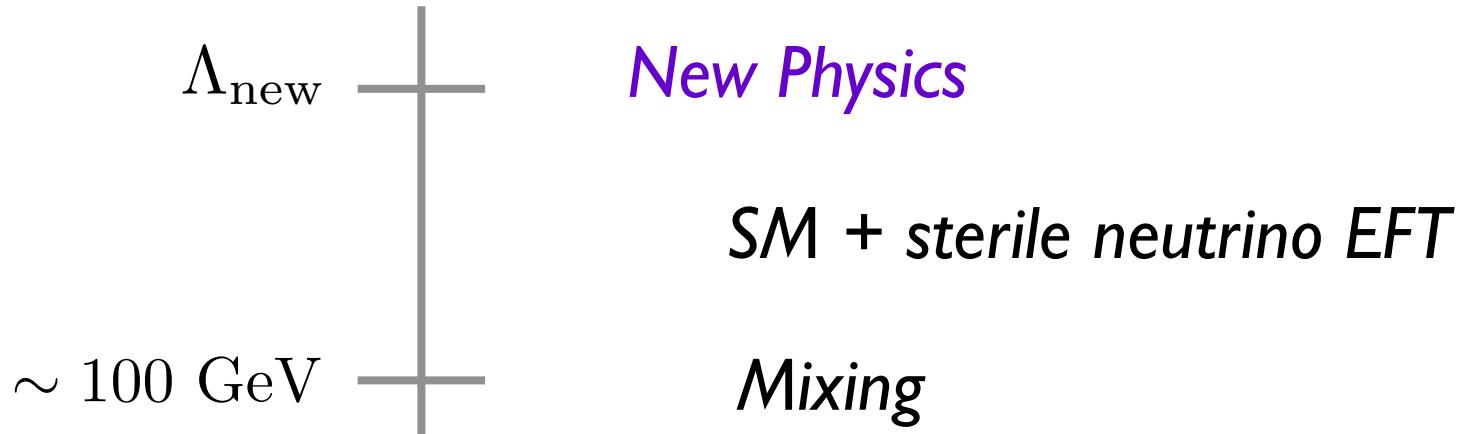
# EFT approach

$\Lambda_{\text{new}}$	$+ \text{New Physics}$
<i>SM + sterile neutrino EFT</i>	
LNC dim 6 operators	
$(\bar{L}\nu_R) \tilde{H} (H^\dagger H)$	$(\bar{d}\gamma^\mu u) (\bar{\nu}_R \gamma_\mu e)$
$(\bar{\nu}_R \gamma^\mu e) (\tilde{H}^\dagger iD_\mu H)$	$(\bar{Q}u) (\bar{\nu}_R L)$
$(\bar{L}\sigma_{\mu\mu}\nu_R) \tau^I \tilde{H} W^I$	$(\bar{L}\nu_R) \epsilon (\bar{Q}_R d)$
	$(\bar{L}d) \epsilon (\bar{Q}_R \nu_R)$
<i>* 7 independent operators</i>	

# EFT approach



# EFT approach



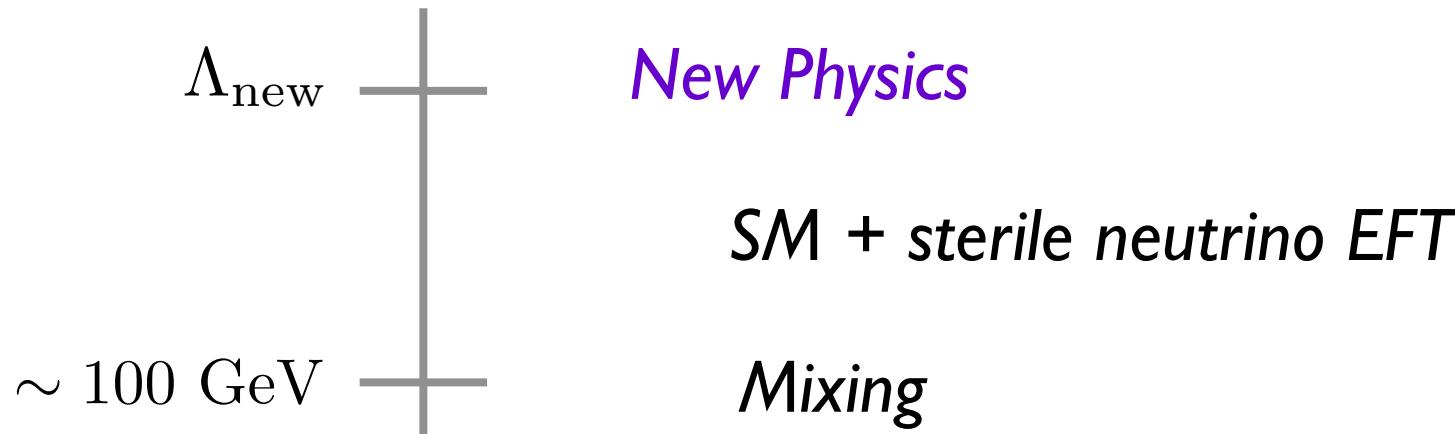
$$\text{Ex)} \quad \mathcal{L}^{(6)} = \frac{G_F}{\sqrt{2}} \left[ \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu C_{\text{VLL}}^{(6)} \nu + \bar{u}_L d_R \bar{e}_L C_{\text{SRR}}^{(6)} \nu \right]$$

$$C_{\text{VLL}}^{(6)} \supset -2 V_{ud} U_{ij} \quad (i = 1, 2, 3)$$

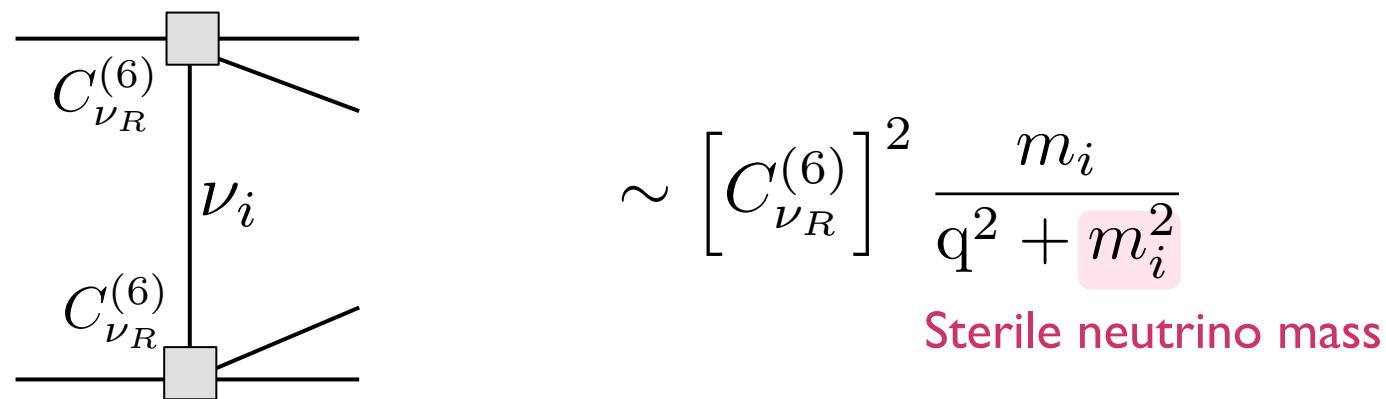
*Unitary matrix*

$$C_{\text{SRR}}^{(6)} \supset \frac{v^2}{2} C_{LdQ\nu}^{(6)} U_{kl}^* \quad \left( \mathcal{O}_{LdQ\nu}^{(6)} = \bar{L}^a d \epsilon_{ab} \bar{Q}_R^b \nu_R \right)$$

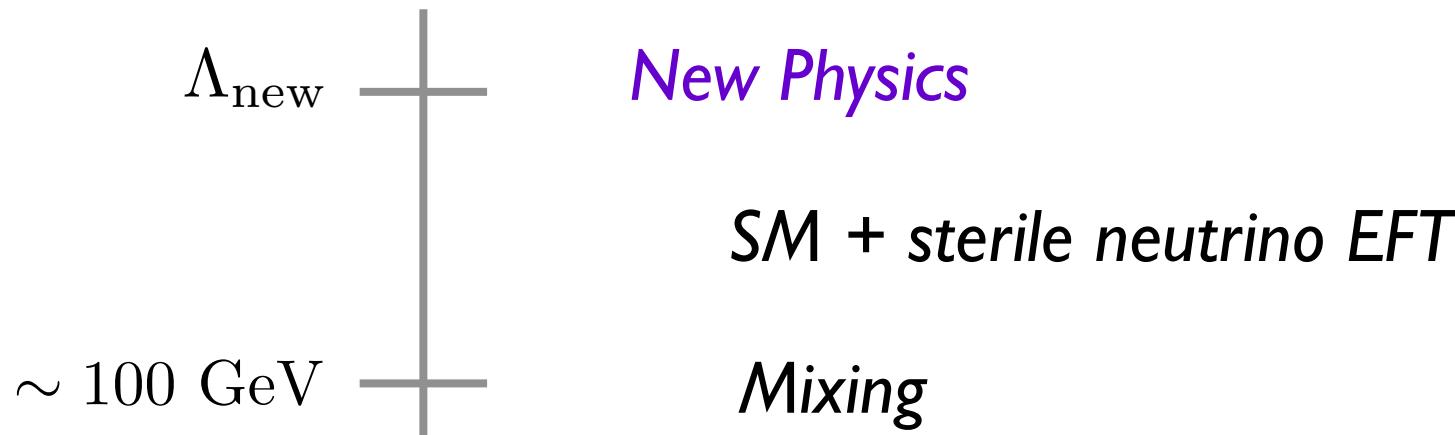
# EFT approach



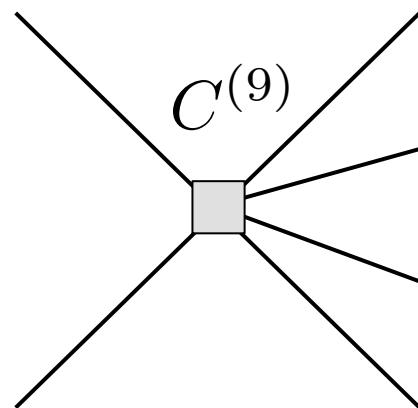
If  $1 \text{ GeV} \lesssim m_i \lesssim v$ ,  $\nu_i$  should also be integrated out.



# EFT approach



If  $1 \text{ GeV} \lesssim m_i \lesssim v$ ,  $\nu_i$  should also be integrated out.



$$C^{(9)} \sim \left[ C_{\nu_R}^{(6)} \right]^2 \frac{1}{m_i}$$

\* Described by Dim 9 operator

# EFT approach

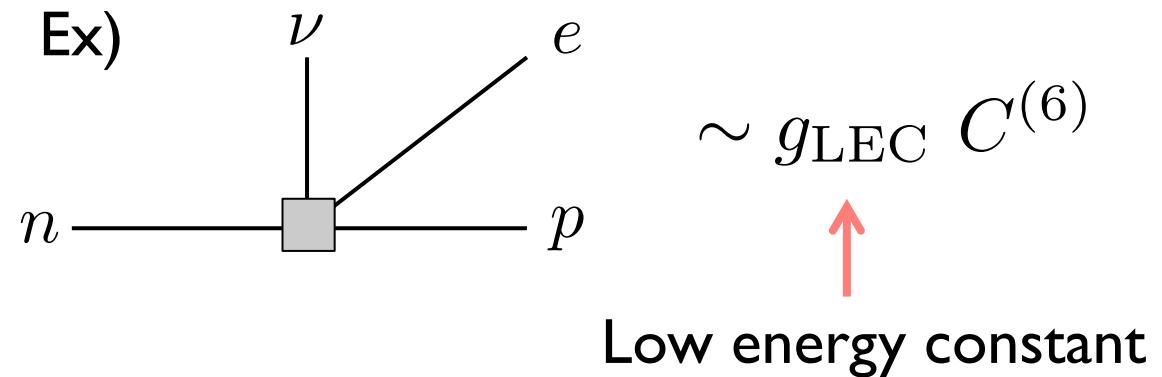
$\sim 1 \text{ GeV}$



*Nucleon and pion interactions*

*~ Chiral Perturbation Theory*

G. Prezeau, M. Ramsey-Musolf, and P. Vogel, PRD68, 034016 (2003)



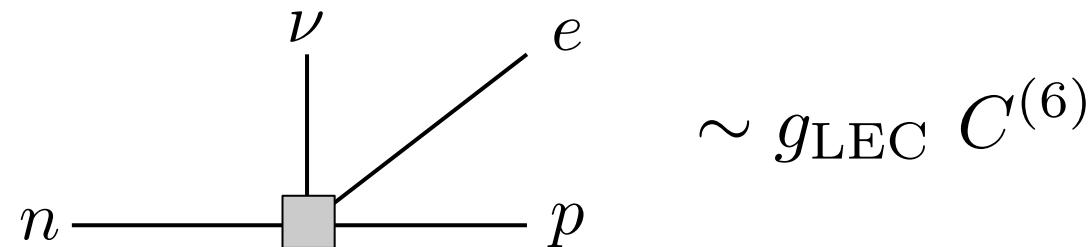
# EFT approach

$\sim 1 \text{ GeV}$

*Nucleon and pion interactions*

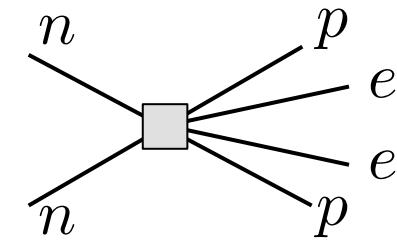
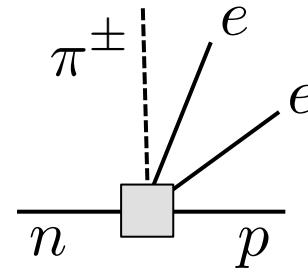
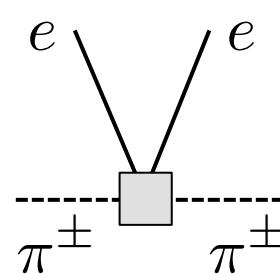
*~ Chiral Perturbation Theory*

G. Prezeau, M. Ramsey-Musolf, and P. Vogel, PRD68, 034016 (2003)



$$\sim g_{\text{LEC}} C^{(6)}$$

*Short-range contributions*

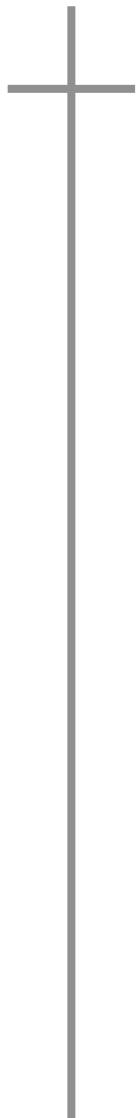


\* Hard-neutrino contributions:

V. Cirigliano, et al., PRL120(2018)20, 202001; PRC100(2019)055504

# EFT approach

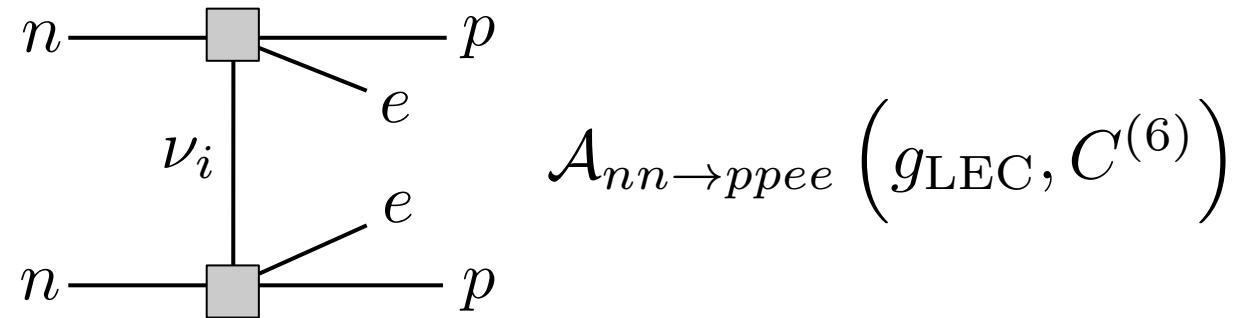
$\sim 1 \text{ GeV}$



*Nucleon and pion interactions*

*~ Chiral Perturbation Theory*

G. Prezeau, M. Ramsey-Musolf, and P. Vogel, PRD68, 034016 (2003)

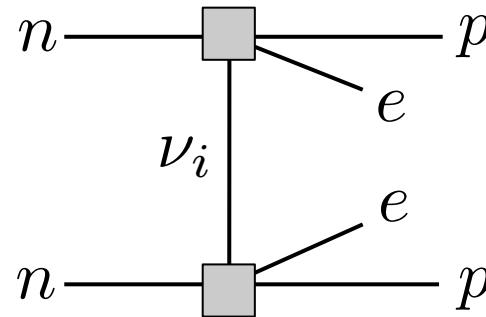


# EFT approach

$\sim 1 \text{ GeV}$

*Nucleon and pion interactions*  
*~ Chiral Perturbation Theory*

G. Prezeau, M. Ramsey-Musolf, and P. Vogel, PRD68, 034016 (2003)



$$\mathcal{A}_{nn \rightarrow pp ee} (g_{\text{LEC}}, C^{(6)})$$

$\sim 1 \text{ MeV}$

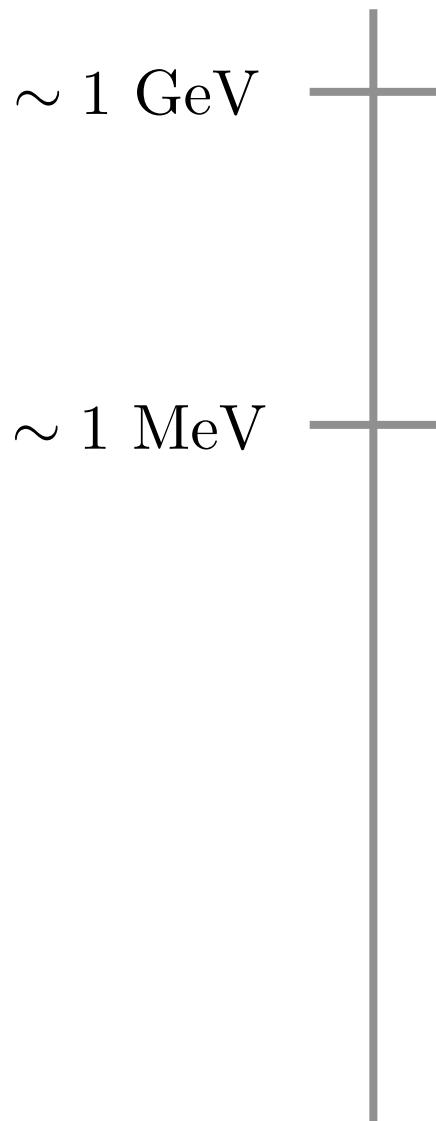
*Transition amplitudes :*

$$\mathcal{A}_{0\nu 2\beta} = \langle 0^+ | \mathcal{A}_{nn \rightarrow pp ee} | 0^+ \rangle$$



Initial and final nuclei states

# EFT approach



*Nucleon and pion interactions*

*$\sim$  Chiral Perturbation Theory*

G. Prezeau, M. Ramsey-Musolf, and P.Vogel, PRD68, 034016 (2003)

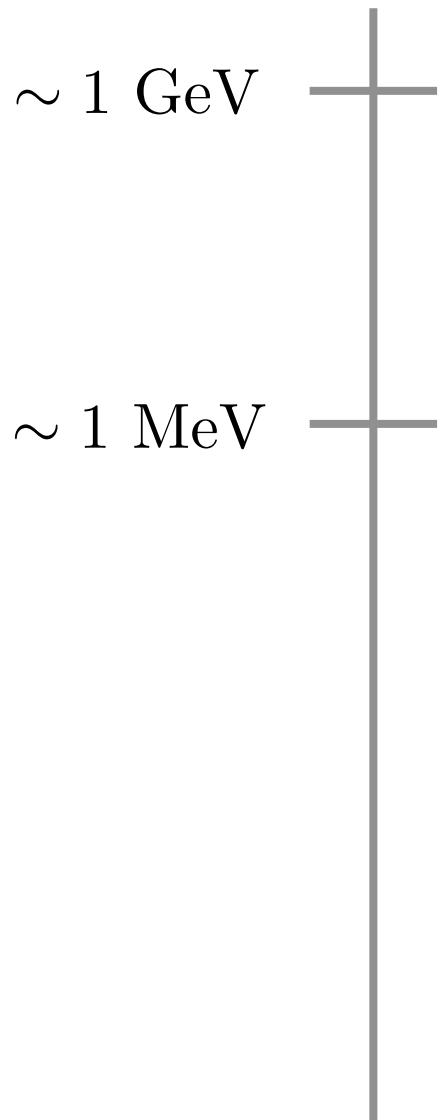
*Transition amplitudes :*

$$\mathcal{A}_{0\nu 2\beta} \left( g_{\text{LEC}}, C^{(6)}, M_{\text{NME}} \right)$$



*Nuclear matrix element  
(Many-body methods )*

# EFT approach



*Nucleon and pion interactions*

*$\sim$  Chiral Perturbation Theory*

G. Prezeau, M. Ramsey-Musolf, and P. Vogel, PRD 68, 034016 (2003)

*Transition amplitudes :*

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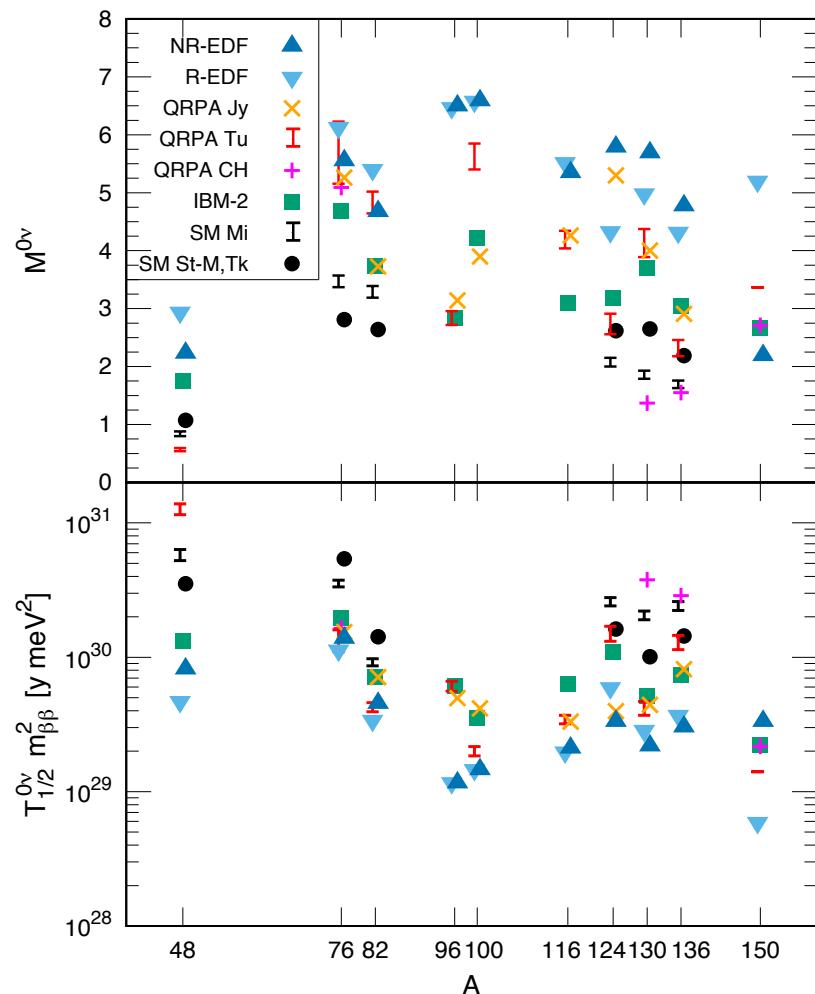
*Inverse half-life :*

$$\left( T_{1/2}^{0\nu} \right)^{-1} = g_A^4 G_{0\nu} |\mathcal{A}_{0\nu 2\beta}|^2$$

$g_A = 1.27$ ,  $G_{0\nu}$  : Phase space factor

# NMEs

NMEs obtained with different nuclear-structure approaches differ by factors of two or three.



J. Engel, J. Menendez  
Rept. Prog. Phys. 80(2017)046301

# LECs

Well determined by experiments or Lattice

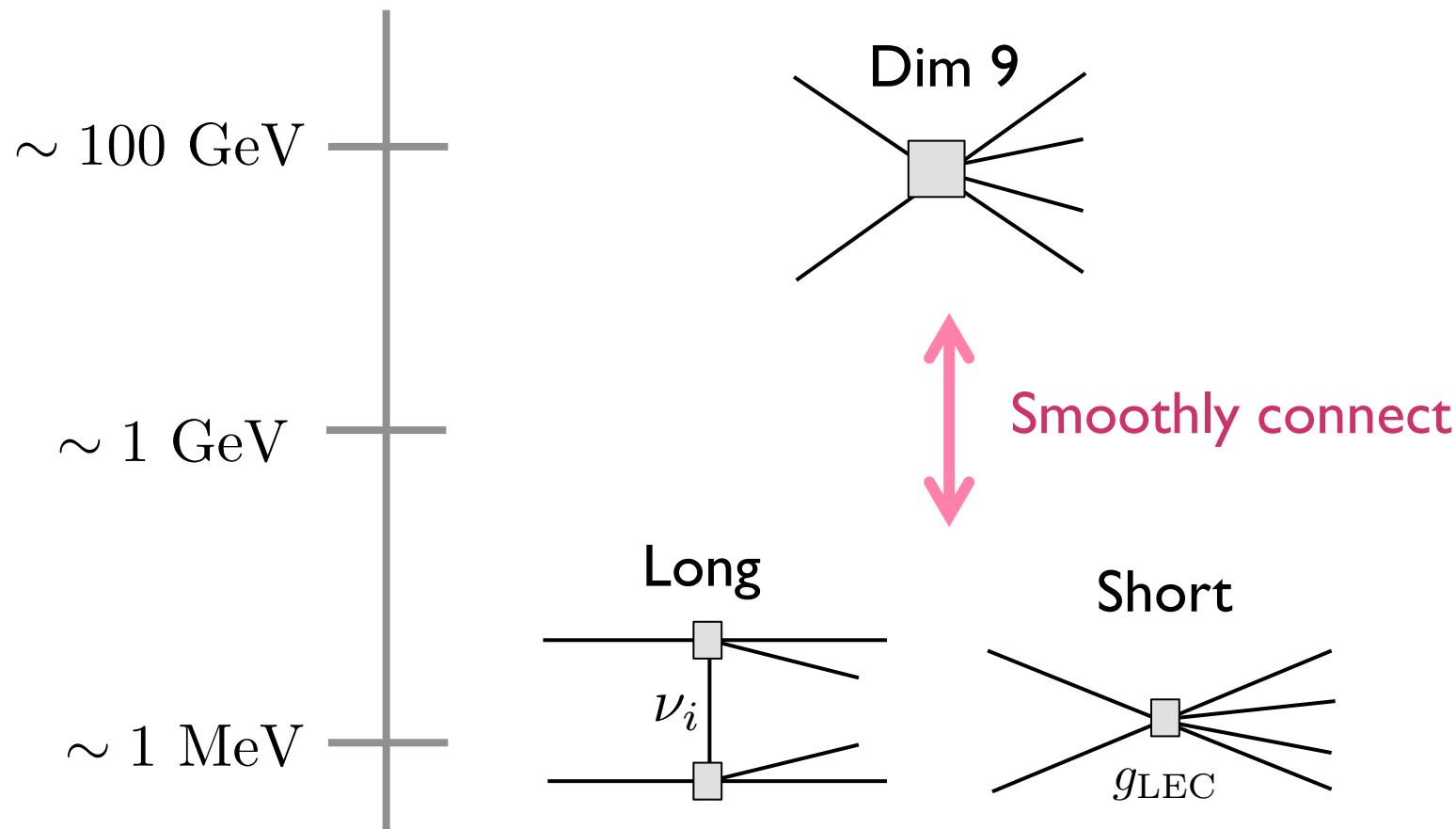
Lattice

$n \rightarrow p e \nu, \pi \rightarrow e \nu$		$\pi\pi \rightarrow ee : \mathcal{O}^{(9)}$	
$g_A$	$1.271 \pm 0.002$ [122]	$g_1^{\pi\pi}$	$0.36 \pm 0.02$ [112]
$g_S$	$1.02 \pm 0.10$ [114, 115]	$g_2^{\pi\pi}$	$2.0 \pm 0.2$ GeV <sup>2</sup> [112]
$g_M$	$4.7$ [122]	$g_3^{\pi\pi}$	$-0.62 \pm 0.06$ GeV <sup>2</sup> [112]
$g_T$	$0.99 \pm 0.03$ [114, 115]	$g_4^{\pi\pi}$	$-1.9 \pm 0.2$ GeV <sup>2</sup> [112]
$ g'_T $	$\mathcal{O}(1)$	$g_5^{\pi\pi}$	$-8.0 \pm 0.6$ GeV <sup>2</sup> [112]
$B$	$2.7$ GeV		
$n \rightarrow p \pi ee : \mathcal{O}^{(9)}, \mathcal{O}^{(6,7)} \otimes \mathcal{O}^{(6,7)}$		$\pi\pi \rightarrow ee : \mathcal{O}^{(6,7)} \otimes \mathcal{O}^{(6,7)}$	
$ g_i^{\pi N} $	$\mathcal{O}(1)$	$ g_{T,VLL}^{\pi\pi} ,  g_{S,VLL}^{\pi\pi} ,  g_{T,VRL}^{\pi\pi} ,  g_{S,VRL}^{\pi\pi} $ $ g_{LR}^{\pi\pi} ,  g_{S1,S2}^{\pi\pi} $ $ g_{TT}^{\pi\pi} ,  g_{TL}^{\pi\pi} ,  g_{TR}^{\pi\pi} $	$\mathcal{O}(1)$ $\mathcal{O}(F_\pi^2)$ $\mathcal{O}(F_\pi^2)$
$nn \rightarrow pp ee : \mathcal{O}^{(9)}$		$nn \rightarrow pp ee : \mathcal{O}^{(6,7)} \otimes \mathcal{O}^{(6,7)}$	
$ g_{1,6,7}^{NN} $	$\mathcal{O}(1)$	$ g_\nu^{NN} ,  g_{LR}^{NN} ,  g_{S1}^{NN} $	$\mathcal{O}(1/F_\pi^2)$
$ g_{2,3,4,5}^{NN} $	$\mathcal{O}((4\pi)^2)$	$ g_{S2}^{NN} ,  g_{TT}^{NN} ,  g_{SLL,VLL}^{NN} $ $ g_{TLL,VLL}^{NN} ,  g_{TL}^{NN} ,  g_{TL,TR}^{NN} $ $ g_{TL,T}^{NN} ,  g_{TR,T}^{NN} $ $ g_{S,VLL}^{NN} ,  g_{T,VLL}^{NN} ,  g_{VLL,VLR}^{NN} $ $ g_{S,VRL}^{NN} ,  g_{T,VRL}^{NN} $ $ g_{T,SRL}^{NN} ,  g_{T,SLL}^{NN} ,  g_{TL,V}^{NN} ,  g_{TR,V}^{NN} $	$\mathcal{O}(1/F_\pi^2)$ $\mathcal{O}(1/F_\pi^2)$ $\mathcal{O}(1/F_\pi^2)$ $\mathcal{O}(1/\Lambda_\chi^2)$ $\mathcal{O}(1)$ $\mathcal{O}(1)$ $\mathcal{O}((4\pi)^2)$

Several LECs are still unknown.

# EFT approach

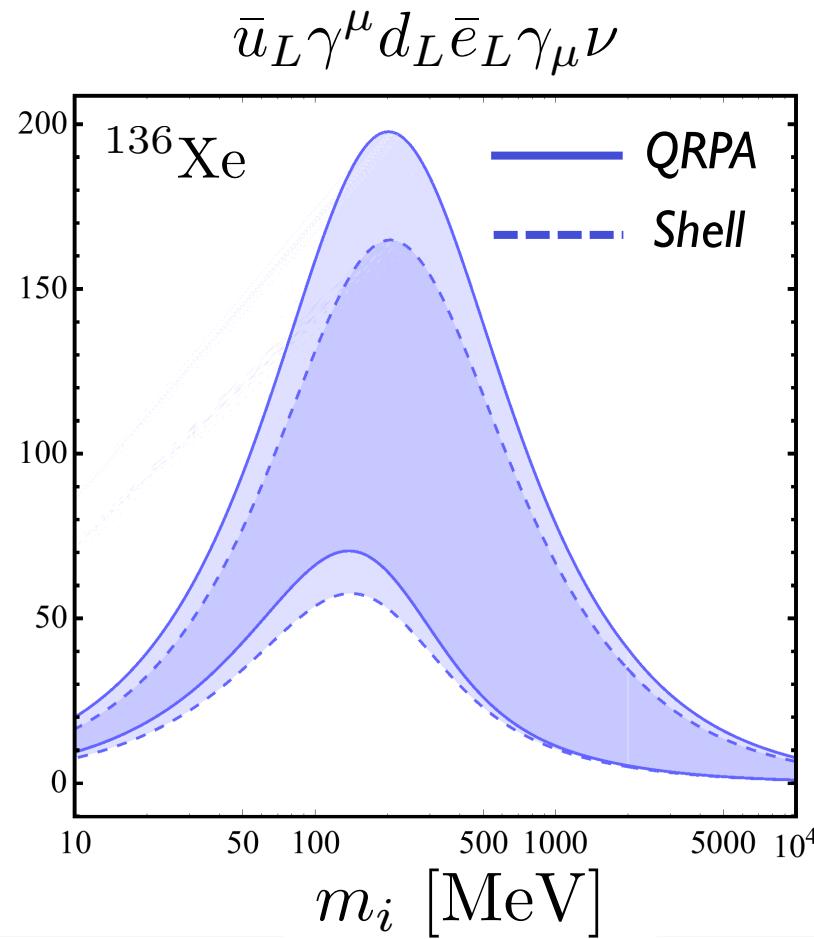
Interpolation formula of  $M_{\text{NME}}(m_i)$  and  $g_{\text{LEC}}(m_i)$



\*This makes it possible to analyze NDBD in any mass spectrum.

# NMEs and LECs

Mass dependence of the amplitude :  $|\mathcal{A}_{0\nu 2\beta}(m_i)|_{^{136}\text{Xe}}$



- Two different NMEs
- Peak around  $\mathcal{O}(100)$  MeV

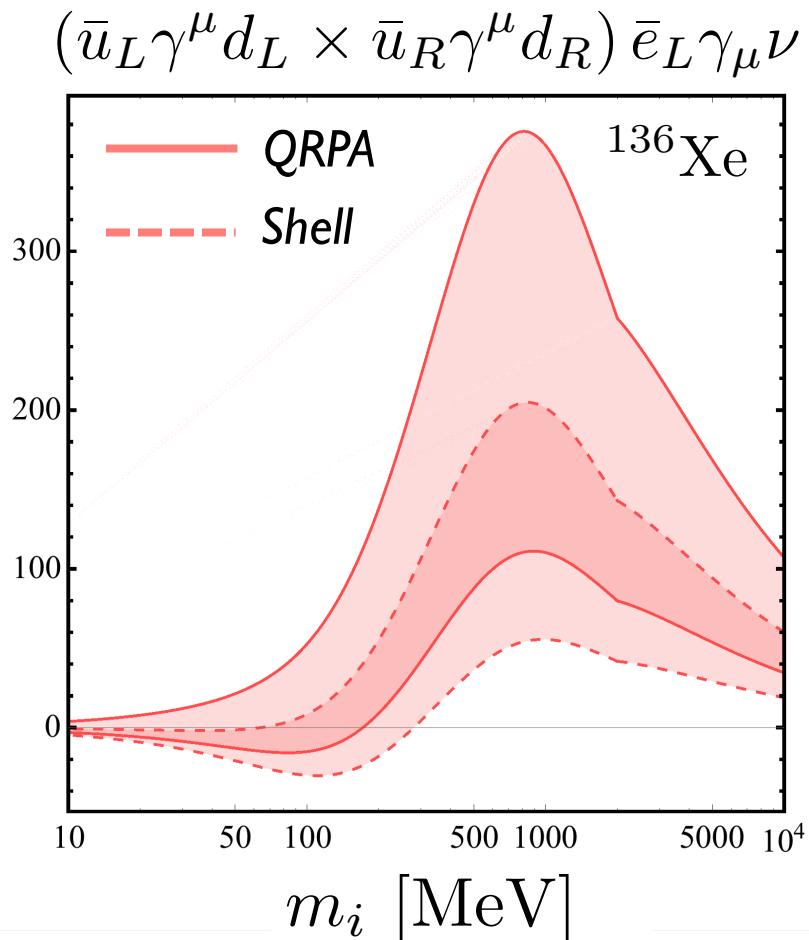
$$\frac{m_i}{q^2 + m_i^2}$$

$\mathcal{O}(100)$  MeV

- Similar behavior in literature  
J.Barea, et al PRD92(2015)093001
- Large uncertainty in LECs

# NMEs and LECs

Mass dependence of the amplitude :  $|\mathcal{A}_{0\nu 2\beta}(m_i)|_{^{136}\text{Xe}}$



- Two different NMEs
- Peak around  $\mathcal{O}(1)$  GeV
  - \* Nontrivial behavior due to LECs
- Not discussed in literature
- Large uncertainty in LECs

*3 + 1 Standard vs Non-standard case  
(Leptoquark)*

## 3+1 scenario

One sterile neutrino :  $m_4$

$$\mathcal{L}_{\nu_R} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \text{H.C}$$

\* Standard interactions

## 3+1 scenario

One sterile neutrino :  $m_4$

$$\mathcal{L}_{\text{mass}} = -\frac{1}{2} \overline{N^c} M_\nu N + \text{h.c.} \quad N = \begin{pmatrix} \nu_L \\ \nu_R^c \end{pmatrix}$$


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Assumption : Two parameters  $M_D$  and  $M_R$

$$M_\nu = \begin{pmatrix} 0 & 0 & 0 & M_D^* \\ 0 & 0 & 0 & M_D^* \\ 0 & 0 & 0 & M_D^* \\ M_D^* & M_D^* & M_D^* & M_R \end{pmatrix}$$

Yukawa

Majorana

$$m_1 = m_2 = 0$$

$$m_{3,4} = \frac{1}{2} \left[ \sqrt{|M_R|^2 + 12|M_D|^2} \pm |M_R| \right] \quad (m_4 > m_3)$$

## 3+1 scenario

One sterile neutrino :  $m_4$

$$\mathcal{L}_{\text{mass}} = -\frac{1}{2} \overline{N^c} M_\nu N + \text{h.c.} \quad N = \begin{pmatrix} \nu_L \\ \nu_R^c \end{pmatrix}$$


---

Assumption : Two parameters  $M_D$  and  $M_R$

$$M_\nu = \begin{pmatrix} 0 & 0 & 0 & M_D^* \\ 0 & 0 & 0 & M_D^* \\ 0 & 0 & 0 & M_D^* \\ M_D^* & M_D^* & M_D^* & M_R \end{pmatrix}$$

Yukawa

Majorana

\* Not satisfy oscillation data but good example  
to understand behaviors of  $0\nu2\beta$

# 3+1 scenario

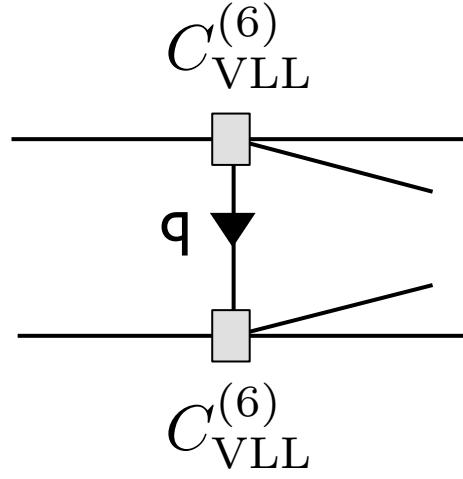
One sterile neutrino :  $m_4$

$$\mathcal{L}^{(6)} = \frac{2G_F}{\sqrt{2}} \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu C_{\text{VLL}}^{(6)} \nu \quad C_{\text{VLL}}^{(6)} = -2V_{ud}U_{ij}$$


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\* *Cancellation of LO contribution in light-mass region*

M. Blennow, et al, JHEP07(2010)096



For  $q^2 \gg m_i^2$

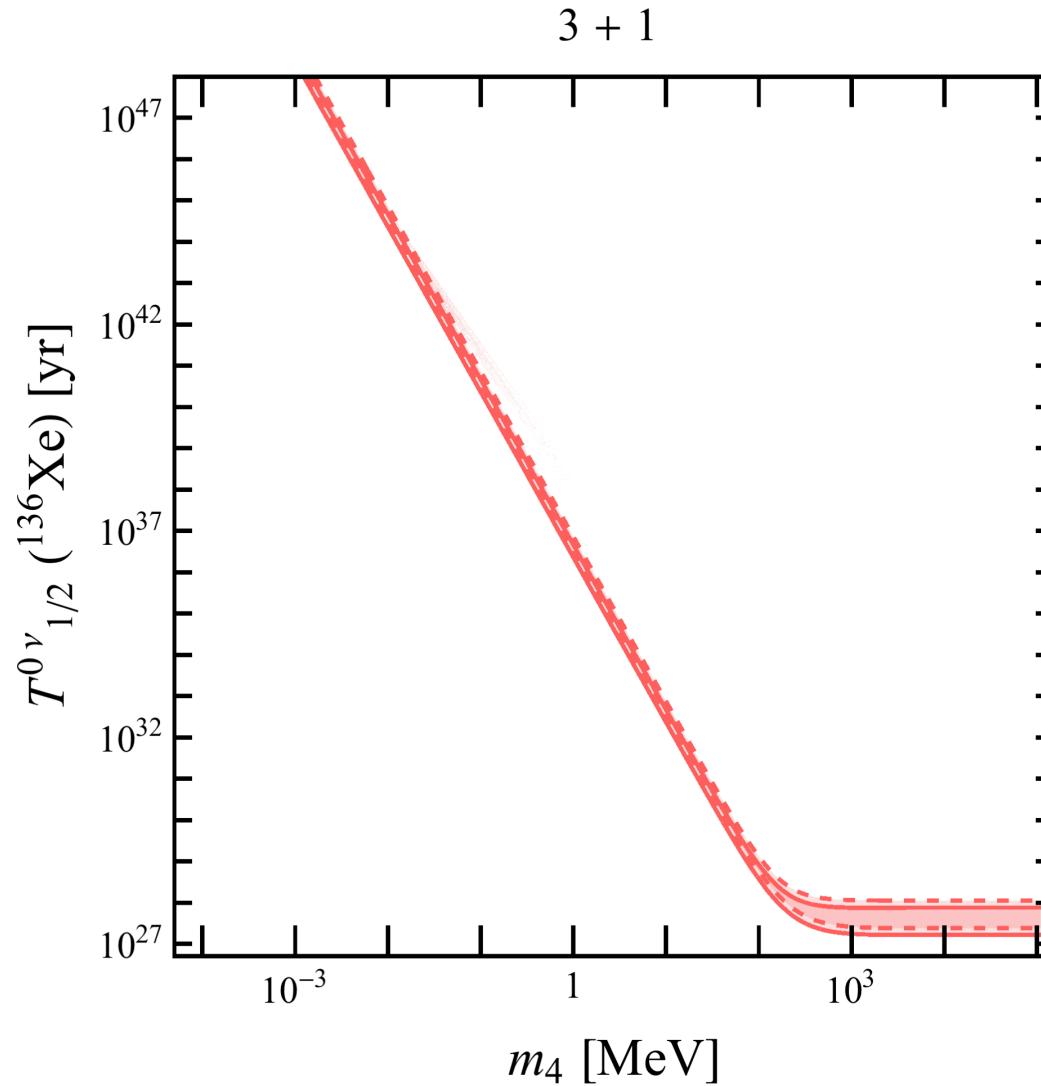
$$\sim \frac{m_i}{q^2} U_{ei}^2 \left( 1 + \frac{m_i^2}{q^2} + \dots \right)$$

↑ LO vanishes

$$q \sim O(100)\text{MeV}$$

$$m_i U_{ei}^2 = (M_\nu)_{11} = 0$$

## $m_4$ vs Half-life ( $^{136}\text{Xe}$ )



The half-life is well above experimental reach.

# Leptoquark

J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 88, 035009 (2013)  
J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 87, 075004 (2013)  
I. Dorsner, S. Fajfer, A. Greljo, J. F. Kamenik and N. Kosnik, Phys. Rept. 641, 1 (2016)

51

Leptoquark (LQ) couples to the SM **quark** and **lepton**  
+ **sterile neutrinos** (1, 2 flavors)

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J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 88, 035009 (2013)  
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I. Dorsner, S. Fajfer, A. Greljo, J. F. Kamenik and N. Kosnik, Phys. Rept. 641, 1 (2016)

52

Leptoquark (LQ) couples to the SM **quark** and **lepton**  
+ **sterile neutrinos** (1, 2 flavors)

*Scalar LQ:*  $\tilde{R} (3, 2, 1/6)$  All possible scalar LQs: PRD43(1991)225

$$\mathcal{L}_{\text{LQ}} = -y^{RL} \bar{d}_R \tilde{R} \epsilon L + y^{\overline{LR}} \bar{Q} \tilde{R} \nu_R$$

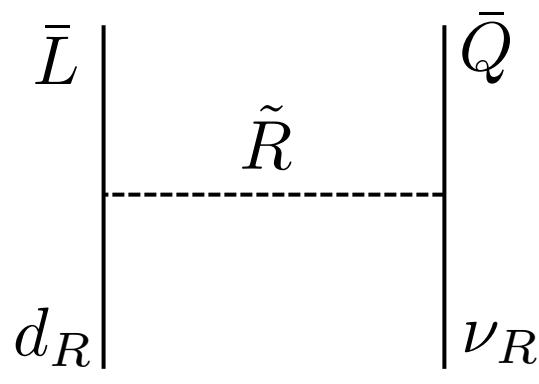
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Gauge-invariant dim6 operator:

$$\mathcal{L}_{\nu_R}^{(6)} = C_{LdQ\nu}^{(6)} (\bar{L} d_R) \epsilon (\bar{Q} \nu_R)$$

$$C_{LdQ\nu}^{(6)} = \frac{1}{m_{LQ}^2} y^{\overline{LR}} y^{RL*}$$

# Leptoquark

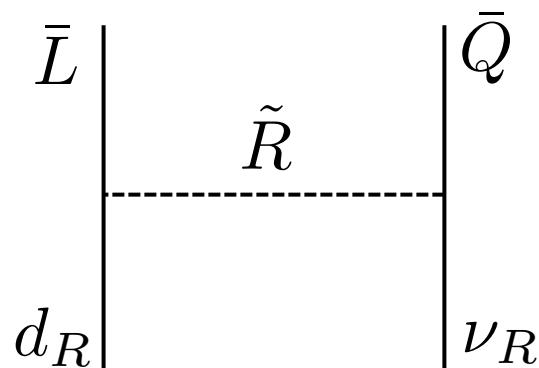
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$$\mathcal{L}_{\text{LQ}} = -y^{RL} \bar{d}_R \tilde{R} \epsilon L + y^{\overline{LR}} \bar{Q} \tilde{R} \nu_R$$



LQ parameters :

$$m_{\text{LQ}} = 10 \text{ TeV} \quad y^{\overline{LR}} y^{RL*} = 1.0$$

# Leptoquark

Scalar and tensor operators show up below EW scale:

$$\mathcal{L}^{(6)} = \frac{2G_F}{\sqrt{2}} \left[ \bar{u}_L d_R \bar{e}_L C_{\text{SRR}}^{(6)} \nu_i + \bar{u}_L \sigma^{\mu\nu} d_R \bar{e}_L \sigma_{\mu\nu} C_{\text{TRR}}^{(6)} \nu_i \right]$$

$$C_{\text{SRR}}^{(6)} = 4C_{\text{TRR}}^{(6)} = \frac{v^2}{2} C_{LdQ\nu}^{(6)} U_{Ni}^* \quad \begin{array}{l} N = 4(5) \\ i = 1 \sim 4(5) \end{array}$$

# Leptoquark

Scalar and tensor operators show up below EW scale:

$$\mathcal{L}^{(6)} = \frac{2G_F}{\sqrt{2}} \left[ \bar{u}_L d_R \bar{e}_L C_{\text{SRR}}^{(6)} \nu_i + \bar{u}_L \sigma^{\mu\nu} d_R \bar{e}_L \sigma_{\mu\nu} C_{\text{TRR}}^{(6)} \nu_i \right]$$

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$$+ \frac{2G_F}{\sqrt{2}} \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu C_{\text{VLL}}^{(6)} \nu \quad \leftarrow \quad \begin{array}{l} \text{Induced by mixing} \\ (\text{No LQ interaction}) \end{array}$$

$$C_{\text{VLL}}^{(6)} = -2V_{ud} U_{ij} \quad i = 1 \sim 3, \ j = 1 \sim 4(5)$$

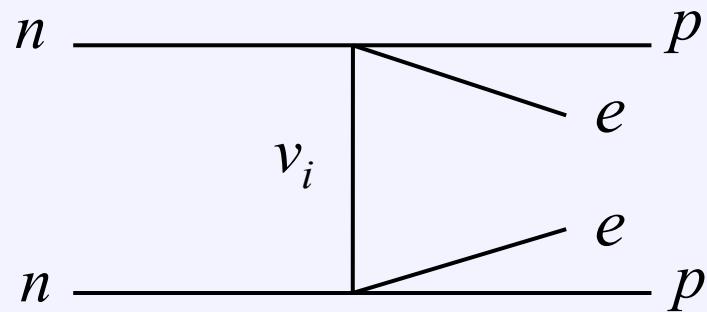
# Leptoquark

Scalar and tensor operators show up below EW scale:

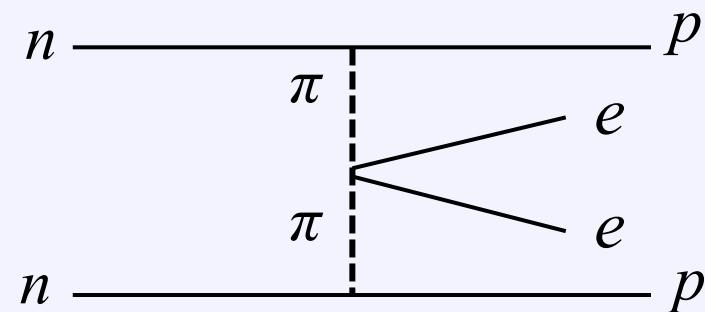
$$\mathcal{L}^{(6)} = \frac{2G_F}{\sqrt{2}} \left[ \bar{u}_L d_R \bar{e}_L C_{\text{SRR}}^{(6)} \nu_i + \bar{u}_L \sigma^{\mu\nu} d_R \bar{e}_L \sigma_{\mu\nu} C_{\text{TRR}}^{(6)} \nu_i \right]$$

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*Neutrino exchange*

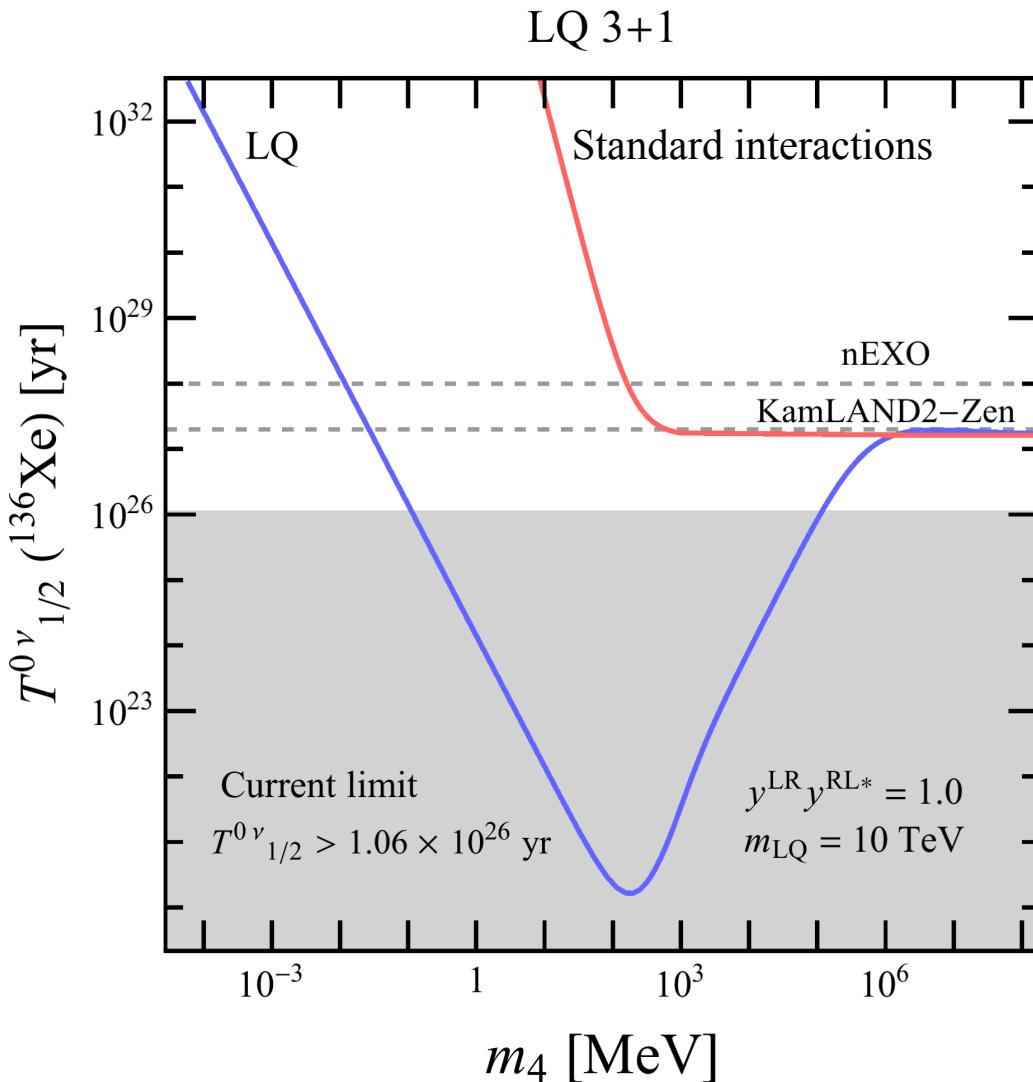


*Pion exchange*

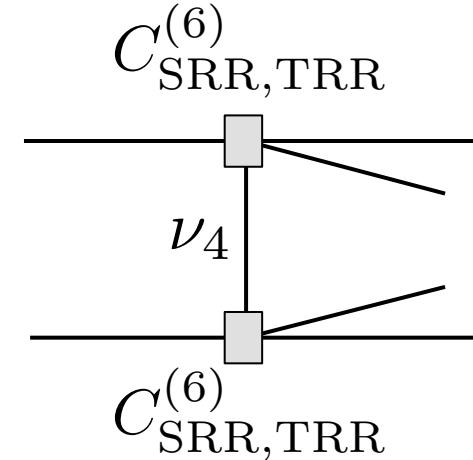


\*  $\pi N$  and  $NN$  interactions are neglected in our analyses.

## 3+1 : $m_4$ vs Half-life



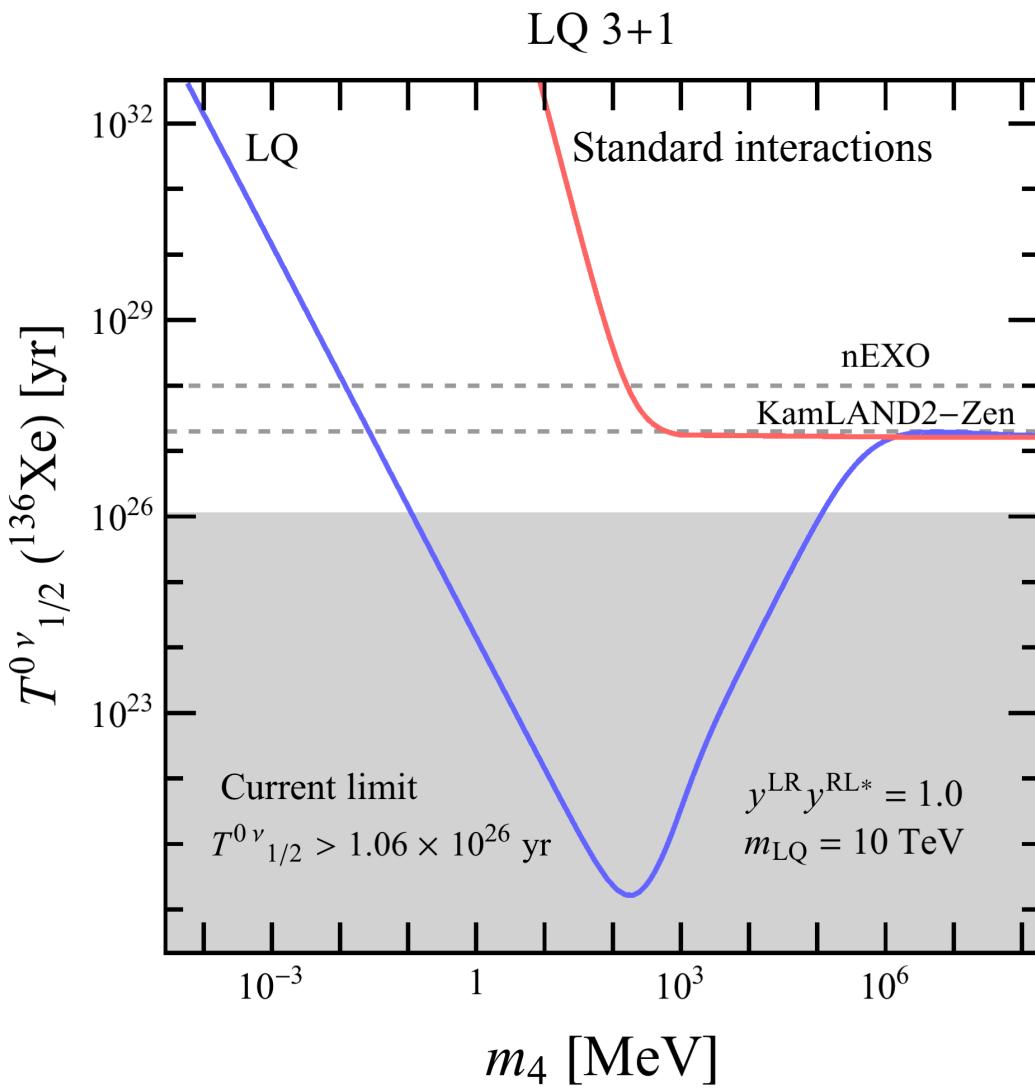
\* *Dominant contribution :  $m_4$*



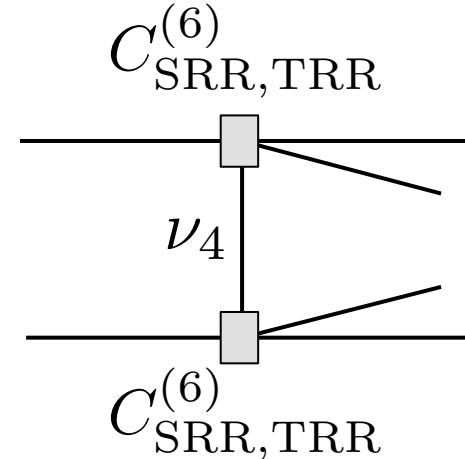
*Pink : No LQ interaction  
 (vector contribution)*

\* *LQ interactions dominate over standard contributions.*

## 3+1 : $m_4$ vs Half-life



\* Dominant contribution :  $m_4$



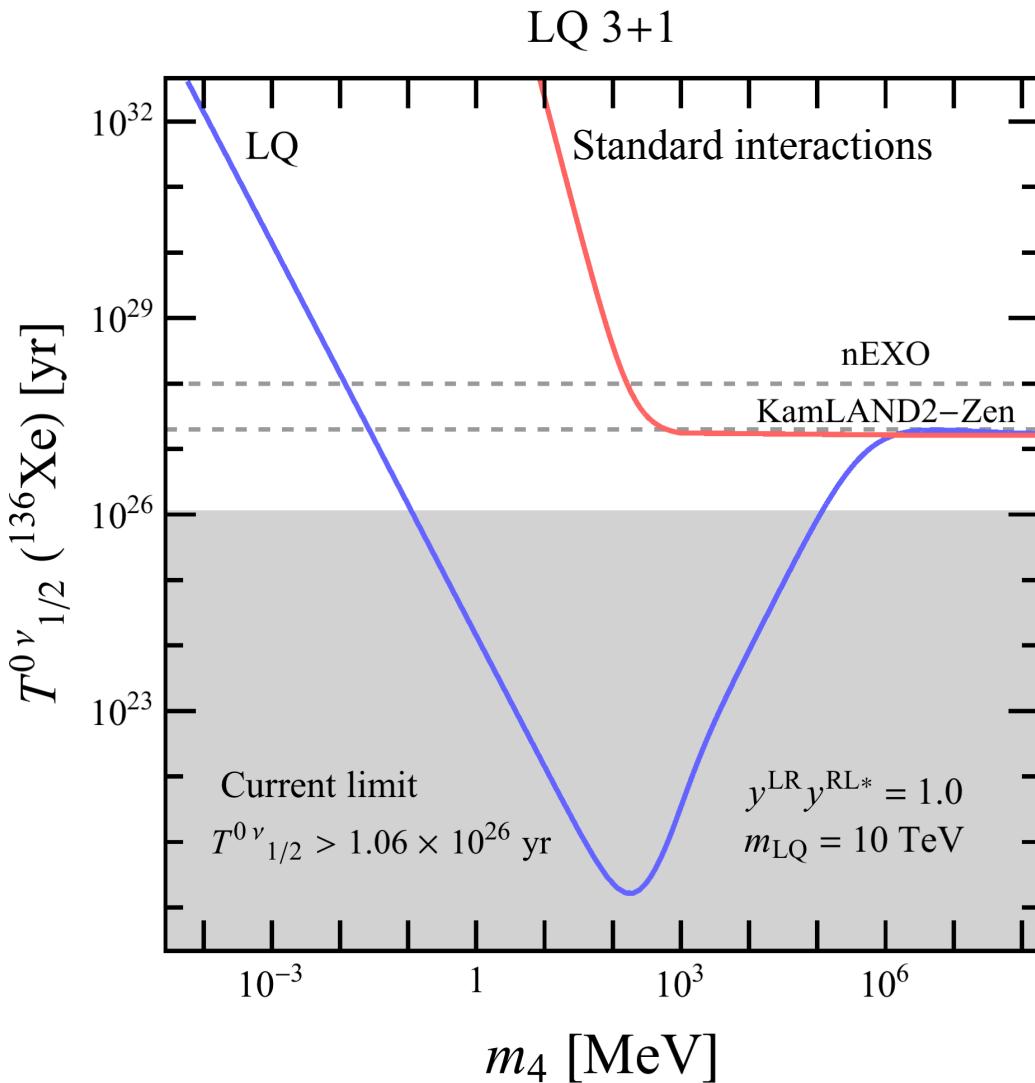
$$T^{0\nu}_{1/2} ({}^{136}\text{Xe}) > 1.06 \times 10^{26} \text{ yr}$$

KamLAND-Zen : PRL117(2016) 082503

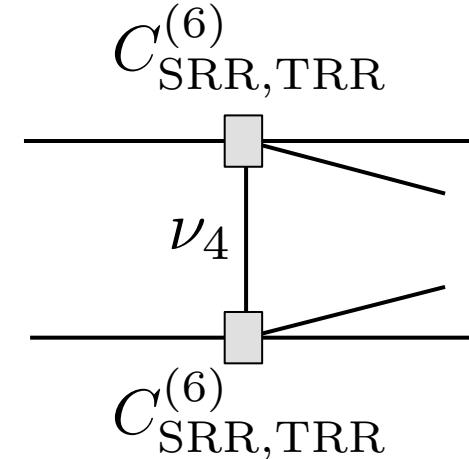
*Ruled out*

$$0.1 \text{ MeV} \lesssim m_4 \lesssim 100 \text{ GeV}$$

# 3+1 : $m_4$ vs Half-life



\* Dominant contribution :  $m_4$



Future sensitivity

$\sim 10^{27}$  yr : KamLAND2-Zen

$\sim 10^{28}$  yr : nEXO

$m_4 \gtrsim 10 \text{ keV}$

*3 + 2 Standard vs Non-standard case  
(Leptoquark)*

## 3 + 2 scenario

Two sterile neutrinos :  $m_4$  and  $m_5$

\* Normal hierarchy is assumed.

Oscillation parameters [PDG] PRD98, 030001(2018) and update (2019)

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$$\Delta m_{21}^2 = 7.39 \cdot 10^{-5} \text{ [eV}^2\text{]} \quad \Delta m_{32}^2 = 2.5 \cdot 10^{-3} \text{ [eV}^2\text{]}$$

$$\sin^2 \theta_{12} = 3.10 \cdot 10^{-1} \quad \sin^2 \theta_{23} = 5.58 \cdot 10^{-1}$$

$$\sin^2 \theta_{13} = 2.241 \cdot 10^{-2} \quad \delta_{\text{Dirac}} = 1.23\pi$$

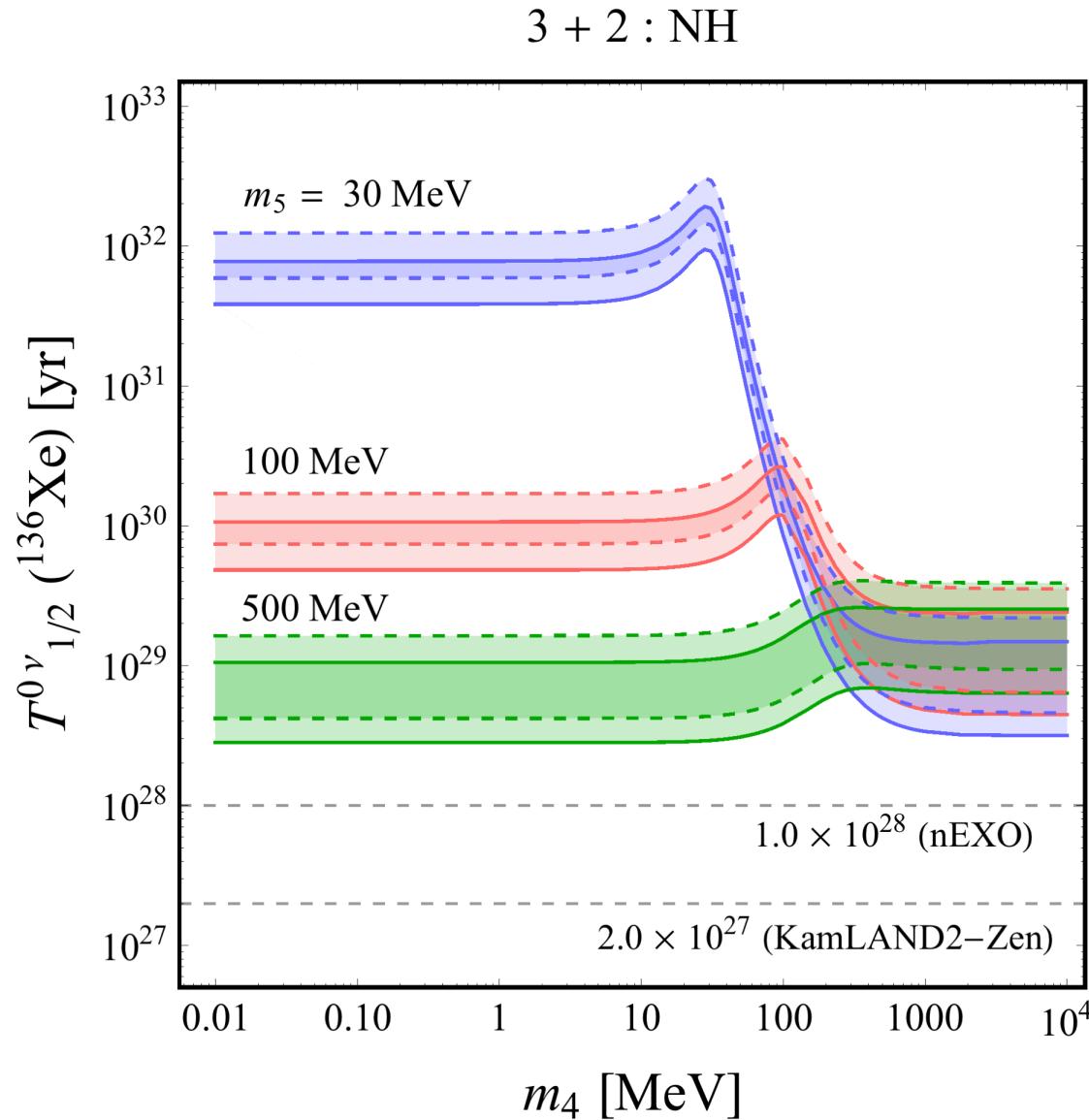

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$$[3+2] \quad \theta_{45} = \pi/8 \quad \gamma_{45} = 0.5 \quad \text{Majorana phases} = 0$$

$m_{4,5}$  : free parameters

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# 3+2 standard : $m_4$ vs Half-life



*Three choices of  $m_5$ :*

*Blue* :  $m_5 = 30 \text{ MeV}$

*Pink* :  $m_5 = 100 \text{ MeV}$

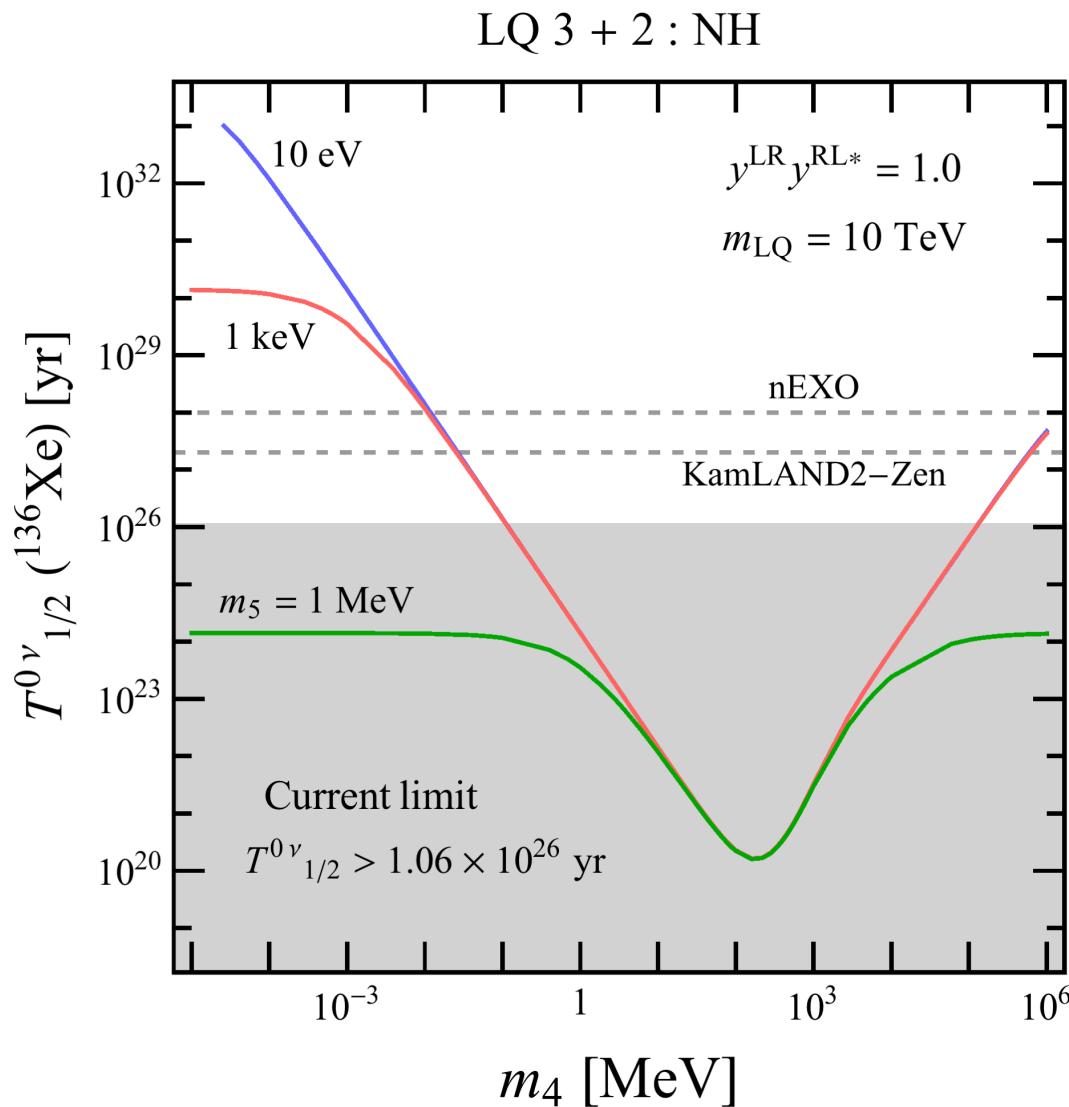
*Green* :  $m_5 = 500 \text{ MeV}$

*Future sensitivity*

$\sim 10^{28} \text{ yr} : \text{nEXO}$

$\sim 10^{27} \text{ yr} : \text{KamLAND2-Zen}$

# 3+2 LQ : $m_4$ vs Half-life



*Three choices of  $m_5$ :*

*Blue* :  $m_5 = 10 \text{ eV}$

*Red* :  $m_5 = 1 \text{ keV}$

*Green* :  $m_5 = 1 \text{ MeV}$

*For the two-light cases,  
the excluded region is*

$0.1 \text{ MeV} \lesssim m_4 \lesssim 100 \text{ GeV}$

# Summary

*Search for neutrinoless double beta decay is a probe of Majorana mass.*

*Sterile neutrinos are motivated by various phenomena.*

$$\text{Mass range : } M_R \quad \text{eV} \longleftrightarrow 10^{15} \text{GeV}$$

**Our study :** Model-independent analyses with light  $\nu_R$

- Possible to analyze NDBD in any mass spectrum with interpolation formulae
- Non-standard interactions can dominate

✓ *Applicable to models with light sterile neutrinos!*