# Neutrinoless Double Beta Decay in the seesaw mechanism 

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Based on collaboration with
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## Introduction

## Neutrino properties

- What are known now ?
- Mixing angles and mass squared differences are measured very precisely by various oscillation experiments

$$
\begin{aligned}
\sin ^{2} \theta_{12} & =0.304_{-0.012}^{+0.012} \\
\sin ^{2} \theta_{23} & =0.573_{-0.020}^{+0.016} \\
\sin ^{2} \theta_{13} & =0.02219_{-0.00063}^{+0.00062}
\end{aligned}
$$

$$
\begin{array}{r}
\Delta m_{21}^{2}=\left(7.42_{-0.20}^{+0.21}\right) \times 10^{-5} \mathrm{eV}^{2} \\
\Delta m_{32}^{2}=\left(2.517_{-0.028}^{+0.026}\right) \times 10^{-3} \mathrm{eV}^{2} \\
\text { for } \mathrm{NH} \text { case }
\end{array}
$$

NuFIT 5.0 (2020)

- What are unknown now ?
- Absolute masses ? (Mass ordering ? Lightest neutrino mass ?)
- Dirac or Majorana fermions ?
- CP violations ? (Dirac phase ? Majorana phase(s) ?)

We do NOT know the mechanism generating neutrino masses !!

## Origin of neutrino masses

- Chiral structure of fermions in the SM

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\]

Why neutrinos are only left-handed?

- Mass spectrum of fermions in the SM


Why neutrinos are are so light?

## Right-handed neutrinos



## Extension by right-handed neutrinos ( $v_{R}$ )

- Seesaw mechanism

Minkowski '77, Yanagida '79, Gell-Mann, Ramond, Slansky '79 Glashow '79

$$
\mathcal{L}=\mathcal{L}_{\mathrm{SM}}+i \overline{v_{R}} \partial_{\mu} \gamma^{\mu} v_{R}-\left(F \bar{L} v_{R} \Phi+\frac{M_{M}}{2} \overline{v_{R}^{c}} v_{R}+h . c .\right)
$$

$$
\begin{gathered}
\mathcal{L} \supset \frac{1}{2}\left(\overline{v_{L}}, \overline{v_{R}^{c}}\right)\left(\begin{array}{cc}
0 & M_{D} \\
M_{D} & M_{M}
\end{array}\right)\binom{v_{L}^{c}}{v_{R}}+\text { h.c. }=\frac{1}{2}\left(\bar{v}, \overline{N^{c}}\right)\left(\begin{array}{cc}
M_{v} & 0 \\
0 & M_{N}
\end{array}\right)\binom{v^{c}}{N}+\text { h.c. } \\
M_{D} \ll M_{M}
\end{gathered}
$$

- Light active neutrinos $v$
- Mass $\quad M_{v}=-M_{D}^{T} \frac{1}{M_{M}} M_{D} \quad\left(M_{v} \ll M_{D}\right)$

Smallness of $M_{\nu}$ is naturally explained
a Heavy neutral leptons (HNLs) $N$

- Mass $M_{N}=M_{M}$ and mixing $\Theta=M_{D} / M_{M}$
- Mixing in weak interaction
- $v_{L}=U v+\Theta N^{c}$



## Scale of seesaw (mass of HNL)

$$
M_{v}=-M_{D}^{T} \frac{1}{M_{M}} M_{D} \boldsymbol{\square} F=\frac{\sqrt{m_{v} M_{N}}}{\langle\Phi\rangle}
$$

$$
m_{v}=5 \times 10^{-11} \mathrm{GeV}
$$



## Mass and mixing of HNL



## Consequences of seesaw mechanism

- Active neutrinos and HNLs are both Majorana fermions
- Lepton number is violated at Lagrangian level
- Crucial for explaining the baryon asymmetry of the Univ.
- Leptogenesis
- Baryogenesis via neutrino oscillation
- Lead to non-SM LNV processes
- Meson decays $\left(B^{-} \rightarrow N \mu^{-} \rightarrow \pi^{+} \mu^{-} \mu^{-}\right)$
- $p p \rightarrow \ell^{+} N \rightarrow \ell^{+} \ell^{+} j j$
- $e^{-} e^{-} \rightarrow W^{-} W^{-}$
- ...
- Neutrinoless Double Beta Decay (NDBD)



## Contents

Today, we discuss

Neutrinoless Double Beta Decay (NDBD) in seesaw mechanism

- Part 1: NDBD in high-scale seesaw
- NDBD in modular flavor symmetry
ref. TA, Yongtae Heo, Takahiro Yoshida (arXiv:2009.12120)
- Part 2: NDBD in low-scale seesaw
- What if NDBD is unseen ?
- What if NDBD is observed ?
ref. TA, Hiroyuki Ishida, Kazuki Tanaka (arXiv:2012.12564, 2012.13527, 2101.12498)
- Summary

Part 1: NDBD in high-scale seesaw

## Effective mass in NDBD decay

- $0 v \beta \beta$ decay rate

$$
\left(T_{1 / 2}^{0 v}\right)^{-1}=G^{0 v}\left|\mathcal{M}^{0 v}\right|^{2}\left|m_{\mathrm{eff}}\right|^{2} \mid
$$

$G^{0 v}$ : Phase space factor
$\mathcal{M}^{0 v}$ : Nuclear matrix element (NME)
$m_{\text {eff }}$ : Effective mass

- Effective mass

$$
m_{\mathrm{eff}}=\sum_{i} U_{e i}^{2} m_{i}
$$


$m_{i}$ : active neutrino masses
$U_{e i}$ : PMNS neutrino mixing element

## Masses and mixings of active neutrinos

- Active neutrino masses $\left(m_{1}, m_{2}, m_{3}\right)$

$m_{3}>m_{2}>m_{1}$


$$
m_{2}>m_{1}>m_{3}
$$

$$
\uparrow \quad v_{2}
$$

$$
v_{1}
$$

$$
v_{3}
$$

- PMNS mixing matrix $\left(\theta_{i j}, \delta, \alpha_{21}, \alpha_{31}\right)$

$$
U=\left(\begin{array}{ccc}
c_{12} c_{13} & s_{12} c_{13} & s_{13} e^{-i \delta} \\
-s_{12} c_{23}-c_{12} s_{23} s_{13} e^{i \delta} & c_{12} c_{23}-s_{12} s_{23} s_{13} e^{i \delta} & s_{23} c_{13} \\
s_{12} s_{23}-c_{12} c_{23} s_{13} e^{i \delta} & -c_{12} s_{23}-s_{12} c_{23} s_{13} e^{i \delta} & c_{23} c_{13}
\end{array}\right)\left(\begin{array}{ccc}
1 & 0 & 0 \\
0 & e^{i \frac{\alpha_{21}}{2}} & 0 \\
0 & 0 & e^{i \frac{\alpha_{31}}{2}}
\end{array}\right)
$$

$$
m_{\mathrm{eff}}=m_{1} c_{12}^{2} c_{13}^{2}+m_{2} s_{12}^{2} c_{13}^{2} e^{i \alpha_{12}}+m_{3} s_{13}^{2} e^{i\left(\alpha_{31}-2 \delta\right)}
$$

## Current status



KamLAND-Zen PRL117, 082503 ('16)


## $0 v \beta \beta$ decay and Majorana phase

- IH case with $\boldsymbol{m}_{2}>\boldsymbol{m}_{1} \gg \boldsymbol{m}_{3}$

$$
m_{\mathrm{eff}} \simeq c_{13}^{2}\left[m_{1}^{2} c_{12}^{4}+m_{2}^{2} s_{12}^{4}+2 \cos \left(\alpha_{21}\right) m_{1} m_{2} c_{12}^{2} s_{12}^{2}\right]^{1 / 2}
$$




Mass ordering, lightest neutrino mass and CPV phases are crucial for estimation of effective mass !

## Flavor Symmetry

- Horizontal symmetry between generations of matter fields can relate elements of Yukawa coupling matrix !

Flavor Symmetry



- So far, various flavor symmetries have been discussed!
- Discrete flavor symmetries
- Flavor mixing can be understood in connection with geometry
- Especially, typical mixing pattern of neutrinos can be explained by S4, A4, $\cdots$ discrete symmetries !

See reviews:
Altarelli, Feruglio ('10), King, Luhn ('13),
Tanimoto ('15), Petcov ('17)

## Origin of Discrete Flavor Symmetry

- Ferglio
- Modular Symmetry in torus compactification is an origin of discrete flavor symmetry.
- Modular Symmetry controls the superpotential leading to the desired mass hierarchies and mixing angles of quarks and leptons

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Kobayashi, Tanaka, Tatsuishi 1803.10391
Penedo, Petcov 1806.11040
Criado, Feruglio 1807.01125
Kobayashi, Omoto, Shimizu, Tanimoto, Tatsuishi 1808.03012
Novichkov, Penedo, Petcov, Titov 1811.04933, 1812.02158
Anda, King, Perdomo 1812.05620
Okada, Tanimoto 1812.09677
Kobayashi, Shimizu, Takagi, Tanimoto, Tatsuishi, Uchida 1812.11072
Novichkov, Petcov, Tanimoto 1812.11289
```


## Modular Symmetry

## Torus compactification

- Torus $\mathbb{C} / \Lambda$

https://commons.wikimedia.org/


$$
\begin{aligned}
& \alpha_{1}=2 \pi R \\
& \alpha_{2}=2 \pi R \tau
\end{aligned}
$$

- Transformations of basis vectors

$$
\begin{aligned}
\binom{\alpha_{2}^{\prime}}{\alpha_{1}^{\prime}} & =\left(\begin{array}{ll}
a & b \\
c & d
\end{array}\right)\binom{\alpha_{2}}{\alpha_{1}}, \quad\left(\begin{array}{ll}
a & b \\
c & d
\end{array}\right) \in S L(2, \mathbb{Z}), \quad S L(2, \mathbb{Z})=\left\{\left.\left(\begin{array}{ll}
a & b \\
c & d
\end{array}\right) \right\rvert\, a, b, c, d \in \mathbb{Z}, a d-b c=1\right\} \\
\tau & \rightarrow \tau^{\prime}=\gamma \tau=\frac{a \tau+b}{c \tau+d}
\end{aligned}
$$

- Modular Symmetry $\bar{\Gamma}$

$$
\bar{\Gamma}=\frac{S L(2, Z)}{\{\mathrm{I},-\mathrm{I}\}}=\operatorname{PSL}(2, Z)
$$

## Modular symmetry

- Modular group is generated by two elements

$$
\begin{array}{r}
S: \tau \rightarrow-1 / \tau \quad S=\left(\begin{array}{cc}
0 & 1 \\
-1 & 0
\end{array}\right) \\
T: \tau \rightarrow \tau+1 \quad T=\left(\begin{array}{ll}
1 & 1 \\
0 & 1
\end{array}\right) \\
\\
S^{2}=1 \text { and }(S T)^{3}=1
\end{array}
$$

- Finite quotient subgroup by imposing $T^{N}=1$

$$
\Gamma_{N}=\left\{S, T \mid S^{2}=\mathbf{1},(S T)^{3}=\mathbf{1}, T^{N}=\mathbf{1}\right\}
$$

- Finite non-Abelian discrete group

$$
\Gamma_{2} \simeq S_{3}, \quad \Gamma_{3} \simeq A_{4}, \quad \Gamma_{4} \simeq S_{4}, \quad \Gamma_{5} \simeq A_{5}, \cdots
$$

These symmetries can play a role of discrete flavor symmetry!

## Chiral matter multiplet

- Modular transformation $\quad \tau \rightarrow \tau^{\prime}=\gamma \tau=\frac{a \tau+b}{c \tau+d}$,

$$
\widehat{\Phi} \rightarrow \widehat{\Phi}^{\prime}=(c \tau+d)^{-k_{\Phi}} \rho_{\Phi}(\gamma) \widehat{\Phi} \quad\left\{\begin{array}{c}
-k_{\Phi}: \text { modular weight } \\
\rho_{\Phi}: \text { representation matrix }
\end{array}\right.
$$

- Superpotential
- Modular invariant terms are obtained by matter multiplets as well as the modular forms.
- Modular forms: holomorphic functions of the modulus $\tau$

$$
Y(\tau) \rightarrow(c \tau+d)^{k_{Y}} \rho_{Y}(\gamma) Y(\tau)
$$

- Modular symmetry restricts the interaction terms in the superpotential, i.e., Yukawa coupling constants !
- Successful descriptions of masses and mixings of fermions

Active research topic !!

TA, Y. Heo, T. Yoshida arXiv:2009.12120

|  | $\hat{L}$ | $\hat{E}_{1}^{c}, \hat{E}_{2}^{c}, \hat{E}_{3}^{c}$ | $\hat{N}^{c}$ | $\hat{H}_{u}$ | $\hat{H}_{d}$ | $\hat{S}$ | $Y^{A_{4}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $S U(2)_{L}$ | $\mathbf{2}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{2}$ | $\mathbf{1}$ | $\mathbf{1}$ |
| $A_{4}$ | $\mathbf{3}$ | $\mathbf{1}, \mathbf{1}^{\prime \prime}, \mathbf{1}^{\prime}$ | $\mathbf{3}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{3}$ | $\mathbf{3}$ |
| M.W. | -1 | -1 | -1 | -1 | -1 | -1 | +2 |
| $R$ | - | - | - | + | + | + | + |

- Introduce a singlet multiplet $\hat{S}$
- Origins of mu-term and Majorana masses

$$
\hat{S}=\left(\begin{array}{l}
\hat{S}_{1} \\
\hat{S}_{2} \\
\hat{S}_{3}
\end{array}\right)
$$

$$
\begin{aligned}
W & =k\left(\hat{S} Y^{A_{4}} \hat{H}_{u} \hat{H}_{d}\right)_{\mathbf{1}} \\
& +h_{1}\left(\left(\hat{S} Y^{A_{4}}\right)_{\mathbf{1}} \hat{N}^{c} \hat{N}^{c}\right)_{\mathbf{1}}+h_{2}\left(\left(\hat{S} Y^{A_{4}}\right)_{\mathbf{1}^{\prime}} \hat{N}^{c} \hat{N}^{c}\right)_{\mathbf{1}}+h_{3}\left(\left(\hat{S} Y^{A_{4}}\right)_{\mathbf{1}^{\prime}} \hat{N}^{c} \hat{N}^{c}\right)_{\mathbf{1}} \\
& +h_{4}\left(\left(\hat{S} Y^{A_{4}}\right)_{\mathbf{3}} \hat{N}^{c} \hat{N}^{c}\right)_{\mathbf{1}}+h_{5}\left(\left(\hat{S} Y^{A_{4}}\right)_{\mathbf{3} \mathbf{a}} \hat{N}^{c} N^{c}\right)_{\mathbf{1}} .
\end{aligned}
$$

- Realistic masses and mixings of neutrinos
$\langle\hat{S}\rangle=\left(\begin{array}{c}S_{1} \\ S_{2} \\ 0\end{array}\right)$


## Superpotential

$$
\begin{aligned}
W & =k\left(\hat{S} Y^{A_{4}} \hat{H}_{u} \hat{H}_{d}\right)_{\mathbf{1}} \\
& +f_{1}\left(\hat{L} Y^{A_{4}}\right)_{\mathbf{1}} \hat{E}_{1}^{c} H_{d}+f_{2}\left(\hat{L} Y^{A_{4}}\right)_{\mathbf{1}^{\prime}} \hat{E}_{2}^{c} H_{d}+f_{3}\left(\hat{L} Y^{A_{4}}\right)_{\mathbf{1}} \hat{E}_{3}^{c} H_{d} \\
& \left.+g_{1}\left(\left(\hat{L} Y^{A_{4}}\right)_{\mathbf{3} \mathbf{s}} \hat{N}^{c} \hat{H}_{u}\right)_{\mathbf{1}}+g_{2}\left(\left(\hat{L} Y^{A_{4}}\right)_{\mathbf{3 a}}\right)_{\mathbf{1}} \hat{N}^{c} \hat{H}_{u}\right)_{\mathbf{1}} \\
& +h_{\mathbf{1}}\left(\left(\hat{S} Y^{A_{4}}\right)_{\mathbf{1}} \hat{N}^{c} \hat{N}^{c}\right)_{\mathbf{1}}+h_{2}\left(\left(\hat{S} Y^{A_{4}}\right)_{\mathbf{1}^{\prime}} \hat{N}^{c} \hat{N}^{c}\right)_{\mathbf{1}}+h_{3}\left(\left(\hat{S} Y^{A_{4}}\right)_{\mathbf{1}^{\prime \prime}} \hat{N}^{c} \hat{N}^{c}\right)_{\mathbf{1}} \\
& +h_{4}\left(\left(\hat{S} Y^{A_{4}}\right)_{\mathbf{3} \mathbf{s}} \hat{N}^{c} \hat{N}^{c}\right)_{\mathbf{1}}+h_{5}\left(\left(\hat{S} Y^{A_{4}}\right)_{\mathbf{3 a}} \hat{N}^{c} N^{c}\right)_{\mathbf{1}} .
\end{aligned}
$$

$$
\begin{aligned}
& Y^{A_{4}}=\left(\begin{array}{l}
1+12 q+36 q^{2}+12 q^{3}+\cdots \\
-6 q^{\frac{1}{3}}\left(1+7 q+8 q^{2}+\cdots\right) \\
-18 q^{\frac{2}{3}}\left(1+2 q+5 q^{2}+\cdots\right)
\end{array}\right. \\
& \left\langle\hat{H}_{d}\right\rangle \quad\left\langle\hat{H}_{u}\right\rangle \quad\langle\hat{S}\rangle=\left(\begin{array}{c}
S_{1} \\
S_{2} \\
0
\end{array}\right)
\end{aligned}
$$

Mass matrices of leptons

$$
\begin{aligned}
& M_{E}=\left\langle\hat{H}_{d}\right\rangle P_{i j k}\left(\begin{array}{ccc}
f_{1} & 0 & 0 \\
0 & f_{2} & 0 \\
0 & 0 & f_{3}
\end{array}\right) \\
& M_{D}=\left\langle\hat{H}_{u}\right\rangle P_{i j k}^{T}\left(\begin{array}{ccc}
2 g_{1} & 0 & 0 \\
0 & 0 & -g_{1}+g_{2} \\
0 & -g_{1}-g_{2} & 0
\end{array}\right) \\
& P_{i j k} \overbrace{\left(e^{c}, \mu^{c}, \tau^{c}\right)}^{\left(\hat{E}_{1}^{c}, \hat{E}_{2}^{c}, \hat{E}_{3}^{c}\right)} \\
& M_{M}=\left(\begin{array}{ccc}
\left(h_{1}+4 h_{4}\right) S_{1} & 0 & \left(h_{2}+h_{4}+h_{5}\right) S_{2} \\
0 & \left(h_{2}-2 h_{4}-2 h_{5}\right) S_{2} & \left(h_{1}-2 h_{4}\right) S_{1} \\
\left(h_{2}+h_{4}+h_{5}\right) S_{2} & \left(h_{1}-2 h_{4}\right) S_{1} & 0
\end{array}\right)
\end{aligned}
$$

Neutrino mass matrix of active neutrinos

$$
M_{v}=-M_{D}^{T} \frac{1}{M_{M}} M_{D}
$$

Seesaw mass matrix of active neutrinos

$$
\left.\begin{array}{rl}
M_{v} & =-M_{D}^{T} M_{M}^{-1} M_{D}=\Lambda\left(\begin{array}{ccc}
1 & b_{2} b_{3} & b_{3} \\
b_{2} b_{3} & b_{1} b_{2} & b_{1} \\
b_{3} & b_{1} & b_{3}^{2}
\end{array}\right)
\end{array}\right) .
$$

## Seesaw mass matrix of active neutrinos

$$
M_{v}=-M_{D}^{T} M_{M}^{-1} M_{D}=\Lambda\left(\begin{array}{ccc}
1 & b_{2} b_{3} & b_{3} \\
b_{2} b_{3} & b_{1} b_{2} & b_{1} \\
b_{3} & b_{1} & b_{3}^{2}
\end{array}\right)
$$

- Described by four parameters


Overall scale of neutrino masses

Mass ratios and mixing angles of neutrinos

- Find parameter range which is consistent with the neutrino oscillation data (3 mixing angles, 2 mass squared differences)


## Prediction: neutrino masses

- Only normal hierarchy fits the neutrino data
- Sum of neutrino masses


Good target for cosmological obs.

$$
\sum m_{i} \geq 0.13 \mathrm{eV}
$$

- Cosmological bound $\sum_{i=1}^{3} m_{i} \leq 0.160 \mathrm{eV}$ [Planck 2018]


Good target for LBL neutrino exp.

## Prediction: Dirac CPV phase

- Clear predictions on CPV phases


T2K Run 1-10 Preliminary


T2K @Neutrino 2020
Slide by P. Dunne

## Prediction: Majorana CPV phases

- Clear predictions on CPV phases




## Neutrinoless double beta decay


$0.037 \mathrm{eV} \leq m_{\text {eff }} \leq 0.047 \mathrm{eV}$

KamLAND-Zen 800 @TAUP2020 Slide by Y. Gando


Good target for KamLAND-Zen 800

## Part 2: NDBD in low-scale seesaw

## NDBD decay in low-scale seesaw

- Both active neutrinos and HNLs contribute to NDBD

$$
\begin{aligned}
\mathcal{M}^{\text {tot }} & =\mathcal{M}^{v} \sum_{i} m_{i} U_{e i}^{2}+\sum_{I} \mathcal{M}^{N}\left(M_{I}\right) M_{I} \Theta_{e I}^{2} \\
& =\mathcal{M}^{v}\left[\sum_{i} m_{i} U_{e i}^{2}+\sum_{I} \frac{\mathcal{M}^{N}\left(M_{I}\right)}{\mathcal{M}^{v}} M_{I} \Theta_{e I}^{2}\right]
\end{aligned}
$$

Effective mass $m_{\text {eff }}$


- Suppression Factor

$$
\underbrace{f_{\beta}\left(M_{I}\right)=\frac{\mathcal{M}^{N}\left(M_{I}\right)}{\mathcal{M}^{v}}=\frac{\Lambda_{\beta}^{2}}{\Lambda_{\beta}^{2}+M_{I}^{2}}}_{\Lambda_{\beta}=\sqrt{\left\langle\vec{p}_{F}^{2}\right\rangle} \sim 200 \mathrm{MeV}}
$$

$$
\begin{aligned}
& \mathcal{M}^{v} \supset \frac{1}{p^{2}-m_{i}^{2}} \simeq \frac{1}{-\left\langle\vec{p}_{F}^{2}\right\rangle} \\
& \mathcal{M}^{N} \supset \frac{1}{p^{2}-M_{I}^{2}} \simeq \frac{1}{-\left(\left\langle\vec{p}_{F}^{2}\right\rangle+M_{I}^{2}\right)}
\end{aligned}
$$

Faessler, Gonzalez, Kovalenko, Simkovic '14 Barea, Kotila, Iachello '15

## Effective mass in low-scale seesaw

- Effective mass

$$
\begin{gathered}
m_{\mathrm{eff}}=\sum_{i=1,2,3} m_{i} U_{e i}^{2} \\
\text { active neutrinos } \boldsymbol{v}_{\mathrm{i}} \\
m_{\mathrm{eff}}^{v} \\
\sum_{I}^{\sum_{\beta} f_{\beta}\left(M_{I}\right) M_{I} \Theta_{e I}^{2}}
\end{gathered}\left\{\begin{array}{l}
f_{\beta}\left(M_{I}\right)=\frac{\Lambda_{\beta}^{2}}{\Lambda_{\beta}^{2}+M_{I}^{2}} \\
\Lambda_{\beta} \sim 200 \mathrm{MeV}
\end{array}\right.
$$

- $N_{\text {I }}$ may give a significant contribution to $m_{\text {eff }}$ !

$$
m_{\mathrm{eff}}^{N}= \begin{cases}M_{I} \Theta_{e I}^{2} & \left(M_{I} \ll \Lambda_{\beta}\right) \\ \frac{\Lambda_{\beta}^{2}}{M_{I}^{2}} M_{I} \Theta_{e I}^{2} & \left(M_{I} \gg \Lambda_{\beta}\right)\end{cases}
$$



## NDBD in low-scale seesaw

- Constraint on the mixing $\left|\Theta_{e l}^{2}\right|$


This bound cannot be applied to some cases in the seesaw mechanism !

## Seesaw relation between mixings

- Neutrino mass matrix

$$
\widehat{M_{v}}=\left(\begin{array}{cc}
0 & M_{D} \\
M_{D}^{T} & M_{M}
\end{array}\right)
$$

$$
0=\left[{\widehat{M_{v}}}\right]_{\alpha \beta}=\left[\widehat{U}{\widehat{M_{\nu}}}^{\text {diag }} \widehat{U}^{T}\right]_{\alpha \beta}
$$



$$
\alpha=\beta=e
$$

$$
0=\sum_{i} m_{i} U_{e i}^{2}+\sum_{I} M_{I} \Theta_{e I}^{2}=m_{\mathrm{eff}}^{v}+\sum_{I} M_{I} \Theta_{e I}^{2}
$$

## When all HNLs are lighter than $\boldsymbol{\Lambda}_{\boldsymbol{\beta}}$

- Effective mass

$$
\begin{array}{rlr}
m_{\mathrm{eff}} & =m_{\mathrm{eff}}^{v}+\sum_{I} f_{\beta}\left(M_{I}\right) M_{I} \Theta_{e I}^{2} & \begin{array}{c}
\text { When } M_{I} \ll \Lambda_{\beta} \\
f_{\beta}\left(M_{I}\right)=1
\end{array} \\
& =m_{\mathrm{eff}}^{v}+\sum_{I} M_{I} \Theta_{e I}^{2} & \\
& =0 & \text { Seesaw relation } \\
0=m_{\mathrm{eff}}^{v}+\sum_{I} M_{I} \Theta_{e I}^{2}
\end{array}
$$

NLDB is hidden by HNLs
even if lepton number is violated in the seesaw mechanism
Cf. We have to include sub-leading corrections (EW loop corr., sub-leading corr. in seesaw etc.)

## When all HNLs are degenerate

- When all heavy neutrinos are degenerate $M_{I}=M_{N}$,

$$
\begin{aligned}
m_{\mathrm{eff}} & =m_{\mathrm{eff}}^{v}+\sum_{I} f_{\beta}\left(M_{I}\right) M_{I} \Theta_{e I}^{2}=m_{\mathrm{eff}}^{v}+f_{\beta}\left(M_{N}\right) \sum_{\perp-=-\infty} M_{N} \Theta_{e I}^{2} \\
& =m_{\mathrm{eff}}^{v}\left[1-f_{\beta}\left(M_{N}\right)\right]
\end{aligned}
$$

TA, Eijima, Ishida '11

- This shows $m_{\text {eff }}$ does not depend on the mixing $\Theta_{e I}$
- Degenerate HNLs give always destructive contribution



## NDBD and HNLs

- HNLs in the seesaw mechanism may give a significant, constructive or destructive contribution to effective mass depending on masses and mixing elements
- What can we learn about HNLs in the seesaw mechanism by forthcoming NDBD experiments ?
- What if NDBD is unseen ?
- What if NDBD is seen ?
- To make a simple discussion, we consider the minimal seesaw model with TWO right-handed neutrinos.

$$
m_{\mathrm{eff}}=m_{\mathrm{eff}}^{v}+f_{\beta}\left(M_{1}\right) M_{1} \Theta_{e 1}^{2}+f_{\beta}\left(M_{2}\right) M_{2} \Theta_{e 2}^{2}
$$

## What if NDBD is unseen?

## HNL may hide NDBD

- Effective mass

$$
m_{\mathrm{eff}}=m_{\mathrm{eff}}^{v}+f_{\beta}\left(M_{1}\right) M_{1} \Theta_{e 1}^{2}+f_{\beta}\left(M_{2}\right) M_{2} \Theta_{e 2}^{2}
$$

- $m_{\text {lightest }}=0$ in the minimal seesaw

$$
\left|m_{\mathrm{eff}}^{v}\right|=\left\{\begin{array}{l}
1.5-3.7 \mathrm{meV}(\mathrm{NH}) \\
19-48 \mathrm{meV}(\mathrm{IH})
\end{array}\right.
$$

- Consider $M_{1} \ll M_{2}$ ( $N_{2}$ decouple)

$$
m_{\mathrm{eff}}=m_{\mathrm{eff}}^{v}+f_{\beta}\left(M_{1}\right) M_{1} \Theta_{e 1}^{2}=0
$$

$\Rightarrow$ NDBD is hidden by HNL contribution

## What's happen ?

## Consequence 1

- Range of mixing element $\left|\Theta_{e 1}\right|^{2}$ is predicted



TA, Ishida, Tanaka arXiv:2012.13186

## Consequence 2

- Flavor structure of mixing elements ( $\left|\Theta_{e 1}\right|^{2},\left|\Theta_{\mu 1}\right|^{2},\left|\Theta_{\tau 1}\right|^{2}$ ) depends on mass ordering and Majorana phase


TA, Ishida, Tanaka arXiv:2012.13186

## What if NDBD is observed?

## HNL may enhance/suppress NDBD

- Effective mass

$$
\begin{aligned}
& m_{\mathrm{eff}}=m_{\mathrm{eff}}^{v}+f_{\beta}\left(M_{1}\right) M_{1} \Theta_{e 1}^{2}+f_{\beta}\left(M_{2}\right) M_{2} \Theta_{e 2}^{2} \\
& \quad \text { Seesaw relation } \quad 0=m_{\text {eff }}^{v}+M_{1} \Theta_{e 1}^{2}+M_{2} \Theta_{e 2}^{2}
\end{aligned}
$$

Hierarchical HNLs $\quad M_{2}>M_{1}$

$$
\Theta_{e 1}^{2}=\frac{m_{\mathrm{eff}}-m_{\mathrm{eff}}^{\nu}\left[1-f_{\beta}\left(M_{2}\right)\right]}{M_{1}\left[f_{\beta}\left(M_{1}\right)-f_{\beta}\left(M_{2}\right)\right]}
$$

- If NDBD is seen at $\left|m_{\text {eff }}\right|=m_{\text {eff }}^{\text {obs },}$


## What's happen ?

## Consequence (Hierarchical HNLs)

- Range of mixing element $\left|\Theta_{e 1}\right|^{2}$ is predicted depending on $m_{\text {eff }}^{\text {obs }}$



KamLAND-Zen

$$
\left|m_{\text {eff }}\right|<(61-165) \mathrm{meV}
$$

## Consequence (Hierarchical HNLs)

- Range of mixing element $\left|\Theta_{e 1}\right|^{2}$ is predicted


TA, Ishida, Tanaka arXiv:2101.12498

## Consequence (Degenerate HNLs)

- Mass and mixing elements are predicted depending on $m_{\text {eff }}^{\text {obs }}$
- $m_{\text {eff }}^{\text {obs }}<\left|\mathrm{m}_{\text {eff }}^{v}\right|$ in the degenerate HNL case



Direct search for degenerate HNLs is difficult

TA, Ishida, Tanaka arXiv:2101.12498


## NDBD in different nuclei

- Effective mass
- Active neutrino contribution

$$
m_{\mathrm{eff}}^{v}=\sum_{i} m_{i} U_{e i}^{2}
$$

independent on decay nuclei
a HNL contribution

$$
\begin{aligned}
m_{\mathrm{eff}}^{N}= & \sum_{I} f_{\beta}\left(M_{I}\right) M_{I} \Theta_{e I}^{2} \quad \text { dependent on decay nuclei ! } \\
& f_{\beta}\left(M_{I}\right)=\frac{\Lambda_{\beta}^{2}}{\Lambda_{\beta}^{2}+M_{I}^{2}}
\end{aligned}
$$

Multiple detection/non-detection by NDBD using different nuclei
is crucial to reveal the properties of HNLs in the seesaw mechanism

## Summary

## Summary

- We have investigated NDBD in the seesaw mechanism
- Active neutrinos and HNLs are both Majorana fermions
- NDBD is an important test of the seesaw mechanism, i.e. to reveal the properties of HNLs (right-handed neutrinos)
- Part 1: NDBD in the high-scale seesaw mechanism
- Active neutrino contribution depends on mass ordering, lightest neutrino mass and CP phases
- Flavor symmetry (e.g. modular symmetry) can restrict the predicted range of the effective mass, which will be faced with near future experiments
- Part 2: NDBD in the low-scale seesaw mechanism
- HNLs can give a significant destructive/constructive effect
- Range of the mixing elements of HNLs can be found, which is a good target for future direct search experiments
- Mass ordering and CP phases can be studied through the flavor structure of the mixing elements of HNLs

